The Cosmic Distance Ladder Terence Tao (UCLA)

Orion nebula, Hubble & Spitzer telescopes, composite image, NASA/JPL

Astrometry

Solar system montage, NASA/JPL



Astrometry is the study of positions and movements of celestial bodies (sun, moon, planets, stars, etc.).

It is a major subfield of astronomy.

Solar system montage, NASA/JPL

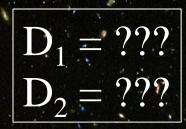
Typical questions in astrometry are:

- How far is it from the Earth to the Moon?
- From the Earth to the Sun?
- From the Sun to other planets?
- From the Sun to nearby stars?
- From the Sun to distant stars?

Solar system montage, NASA/JPL

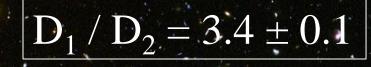
These distances are far too vast to be measured directly.

 D_2



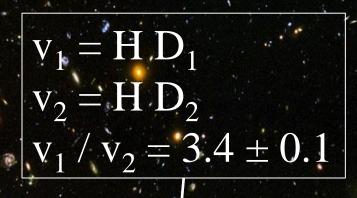
Hubble deep field, NASA/ESA

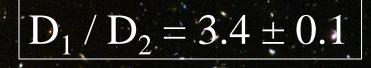
Nevertheless, there are several ways to measure these distances indirectly.



Hubble deep field, NASA/ESA

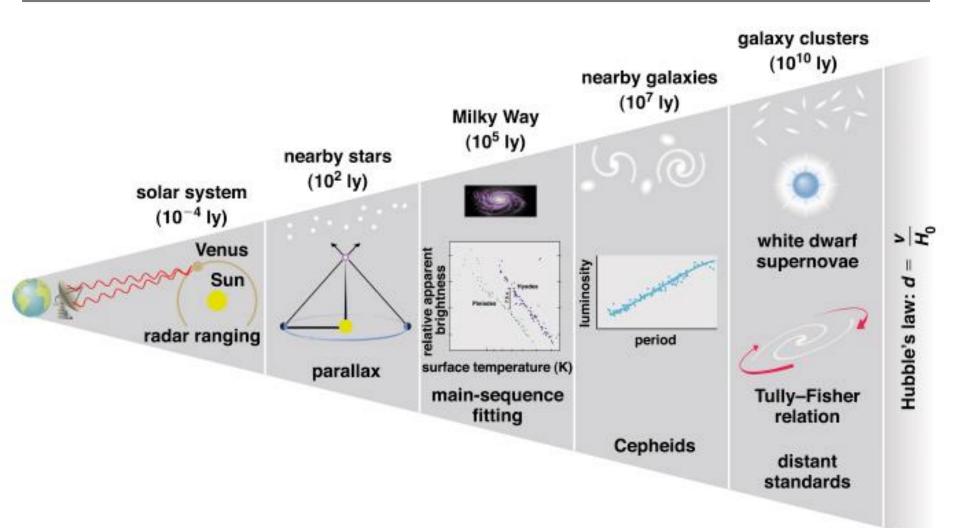
The methods often rely more on mathematics than on technology.



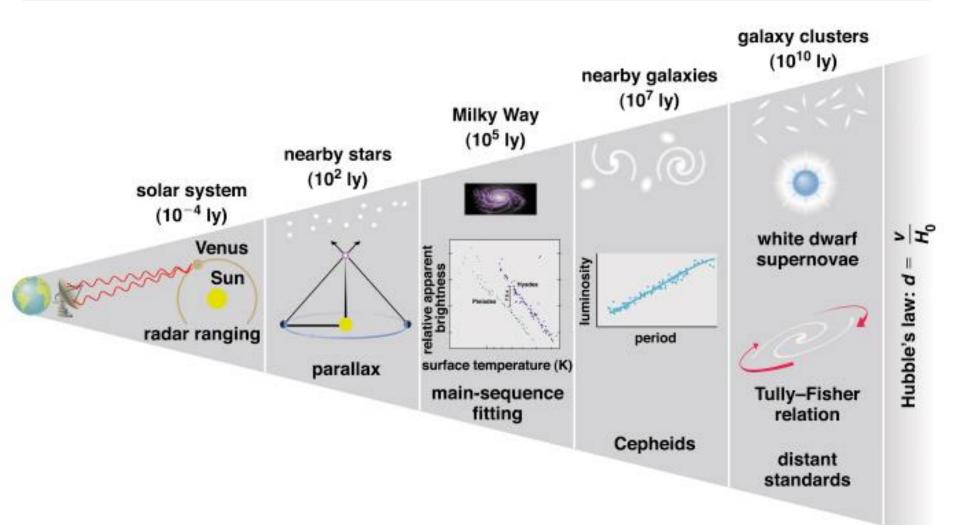


Hubble deep field, NASA/ESA

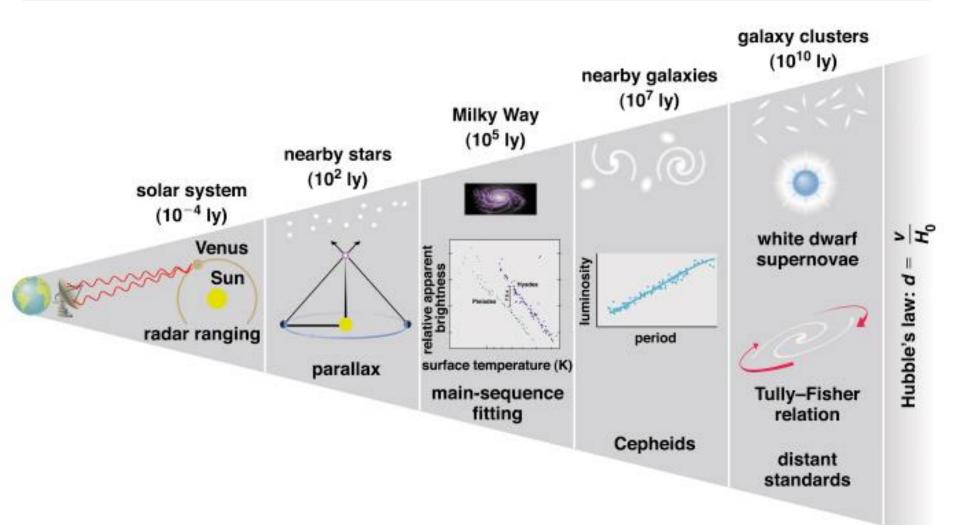
The indirect methods control large distances in terms of smaller distances.



The smaller distances are controlled by even smaller distances...



... and so on, until one reaches distances that one can measure directly.



This is the cosmic distance ladder. galaxy clusters (10¹⁰ ly) nearby galaxies (107 ly) Milky Way (10⁵ ly) nearby stars (10^2 ly) solar system (10^{-4} ly) > Lo white dwarf Venus supernovae uminosity Hubble's law: d = Sun brightno radar ranging period surface temperature (K) parallax main-sequence Tully-Fisher fitting relation Cepheids distant standards

1st rung: the Earth

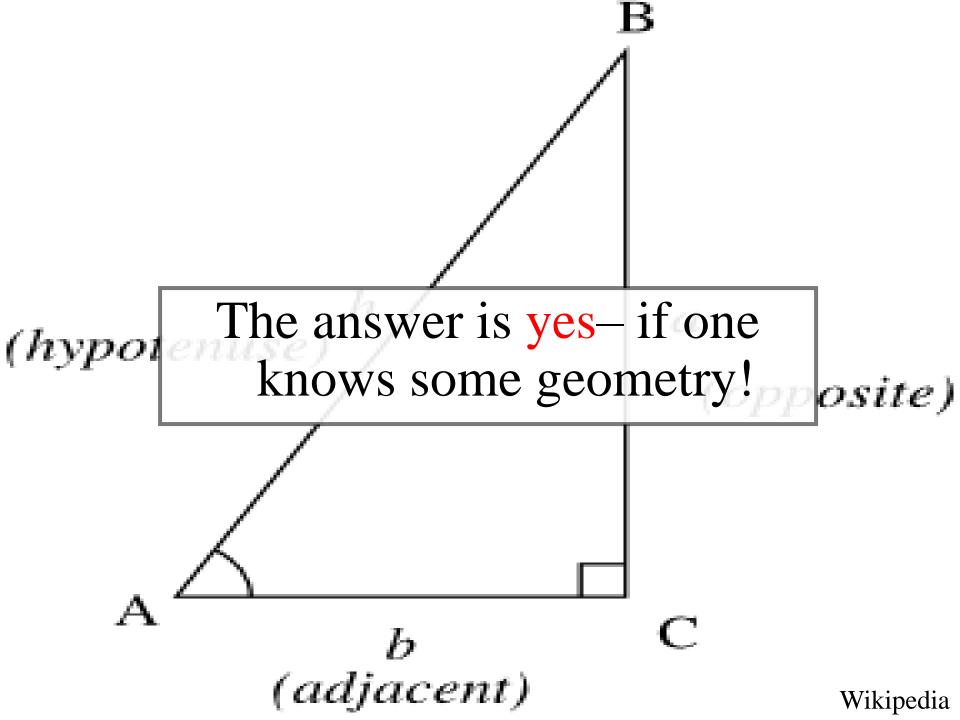
Nowadays, we know that the earth is approximately spherical, with radius 6378 kilometers (3963 mi) at the equator and 6356 kilometers (3949 mi) at the poles.

These values have now been verified to great precision by many means, including modern satellites.

But suppose we had no advanced technology such as spaceflight, ocean and air travel, or even telescopes and sextants.

Could we still calculate the radius of the Earth?

Could we even tell that the Earth was round?





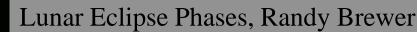
Aristotle (384-322 BCE) gave a convincing indirect argument that the Earth was round... by looking at the Moon.

Copy of a bust of Aristotle by Lysippos (330 BCE)



Aristotle knew that lunar eclipses only occurred when the Moon was directly opposite the Sun.

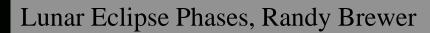






He deduced that these eclipses were caused by the Moon falling into the Earth's shadow.

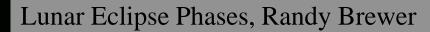






But the shadow of the Earth on the Moon in an eclipse was always a circular arc.

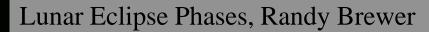






In order for Earth's shadows to always be circular, the Earth must be round.





Aristotle also knew there were stars one could see in Egypt but not in Greece.

Night Sky, Till Credner

He reasoned that this was due to the curvature of the Earth, so that its radius was finite.

Night Sky, Till Credner

However, he was unable to get an accurate measurement of this radius.

Night Sky, Till Credner

Eratosthenes (276-194 BCE) computed the radius of the Earth to be 40,000 stadia (6800 km, or 4200 mi).

Eratosthenes, Nordisk familjebok, 1907

This is accurate to within eight percent.

Eratosthenes, Nordisk familjebok, 1907

The argument was again indirect – but now relied on looking at the Sun.

Eratosthenes, Nordisk familjebok, 1907

Eratosthenes read of a well in Syene, Egypt which at noon on the summer solstice (June 21) would reflect the overhead sun.



[This is because Syene lies almost directly on the Tropic of Cancer.]



Eratosthenes tried the same experiment in his home city of Alexandria.



But on the solstice, the sun was at an angle and did not reflect from the bottom of the well.



Using a gnomon (measuring stick), Eratosthenes measured the deviation of the sun from the vertical as 7°.



From trade caravans and other sources, Eratosthenes knew Syene to be 5,000 stadia (740 km) south of Alexandria.



This is enough information to compute the radius of the Earth.



[This assumes that the Sun is quite far away, but more on this later.]



Tropic of Cancer: Swinburne University, COSMOS Encyclopedia of Astronomy

2nd rung: the Moon



What shape is the Moon? How large is the Moon? How far away is the Moon?

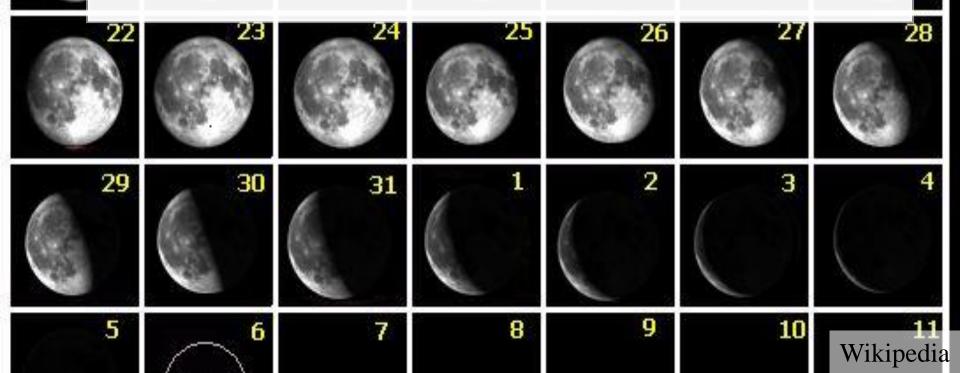
The ancient Greeks could answer these questions also.



Monday Tuesday Wednesday Thursday Friday Saturday
Aristotle argued that the Moon was a sphere (rather than a disk) because the terminator (the boundary of the Sun's light on the Moon) was always an elliptical arc.

Sunday

ne



Aristarchus (310-230 BCE) computed the distance of the Earth to the Moon as about 60 Earth radii. [In truth, it varies from 57 to 63 Earth radii.]



Aristarchus also computed the radius of the Moon as 1/3 the radius of the Earth.

[In truth, it is 0.273 Earth radii.]

Bust of Aristarchus - NASA

The radius of the Earth was computed in the previous rung of the ladder, so we now know the size and location of the Moon.

Radius of moon = 0.273 radius of Earth = 1,700 km = 1,100 mi Distance to moon = 60 Earth radii = 384,000 km = 239,000 mi

Bust of Aristarchus - NASA



Aristarchus's argument to measure the distance to the Moon was indirect, and relied on the Sun.

Sun





Aristarchus knew that lunar eclipses were caused by the Moon passing through the Earth's shadow.

Sun





The Earth's shadow is approximately two Earth radii wide*.

2r

Sun

* This is an oversimplification; there is a correction due to the angular width of the Sun.

Wikipedia



Orbit of the M

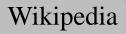
v = 2r / 3 hours

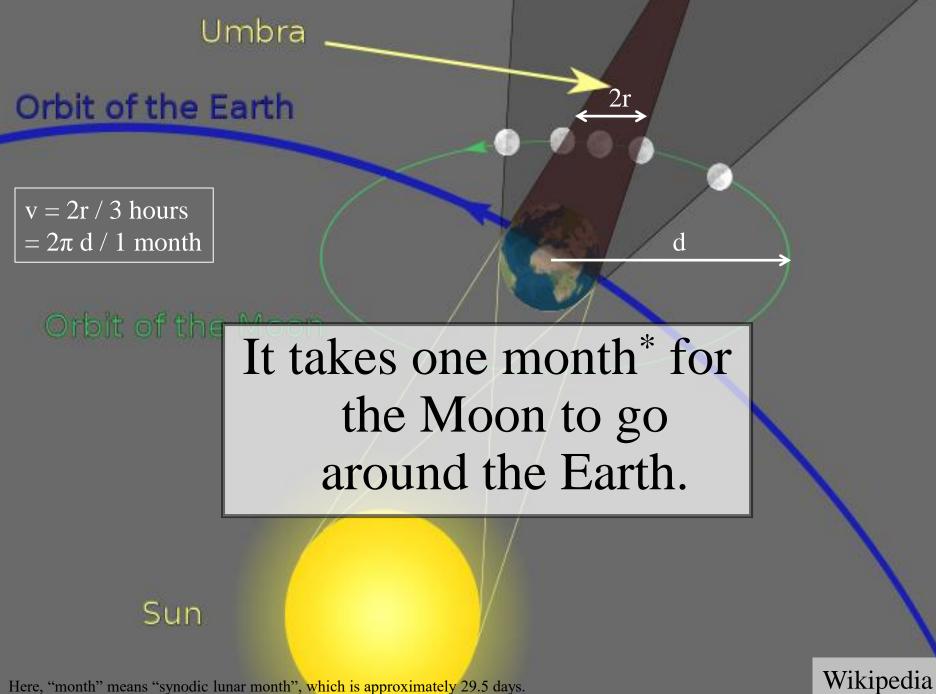
The maximum length of a lunar eclipse is three hours*.

ZĽ

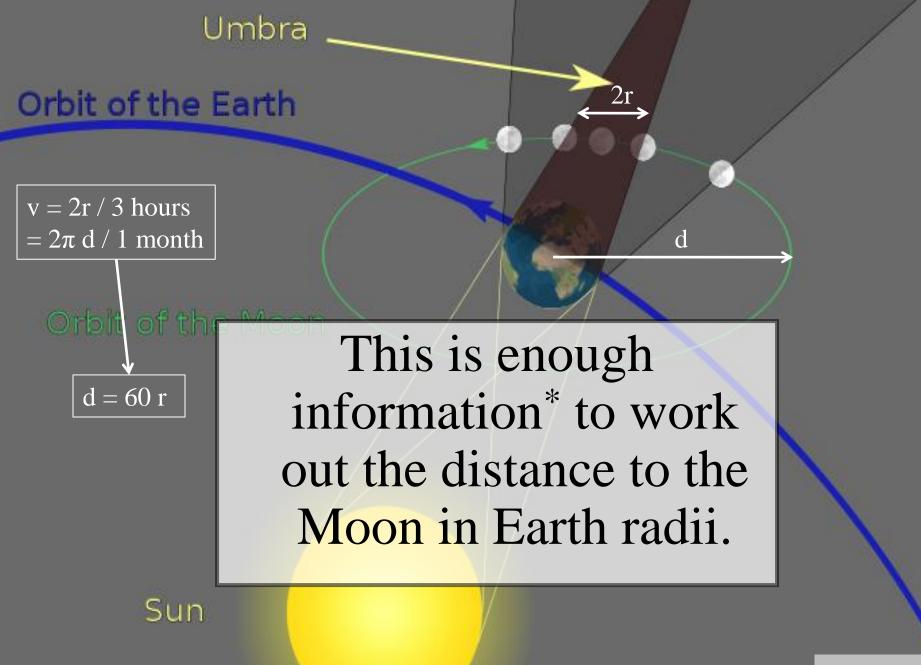


* More precisely, the center of the Moon stays in the umbra for at most 3 hours.





* Here, "month" means "synodic lunar month", which is approximately 29.5 days.



* The actual calculation is more complicated than the above equations suggest, due to the previous footnotes.

Wikipedia

 $\overline{V} = 2\overline{R}/2 \min$

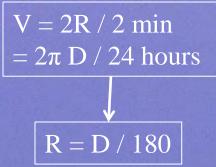
Also, the Moon takes about 2 minutes to set.

 $2\mathbf{R}$

V = 2R / 2 min $= 2\pi d / 24 hours$

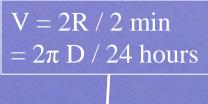
The Moon takes 24 hours to make a full (apparent) rotation around the Earth.

 $2\mathbf{R}$



This is enough information to determine the radius of the Moon, in terms of the distance to the Moon...

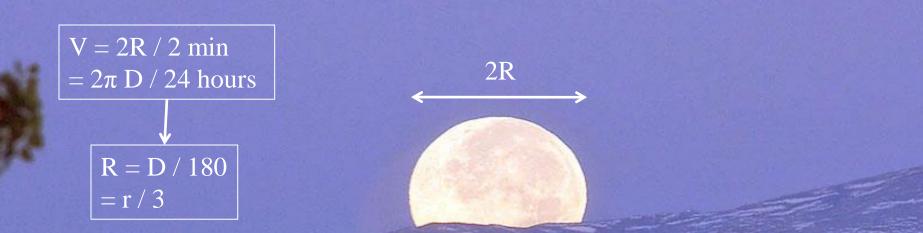
 $2\mathbf{R}$



 $\begin{vmatrix} \mathbf{R} &= \mathbf{D} / 180 \\ = \mathbf{r} / 3 \end{vmatrix}$

.. which we have just computed.

 $2\mathbf{R}$



[Aristarchus, by the way, was handicapped by not having an accurate value of π, which had to wait until Archimedes (287-212BCE) some decades later!]

3rd rung: the Sun

How large is the Sun? How far away is the Sun?

Once again, the ancient Greeks could answer these questions (but with imperfect accuracy).

Their methods were indirect, and relied on the Moon.

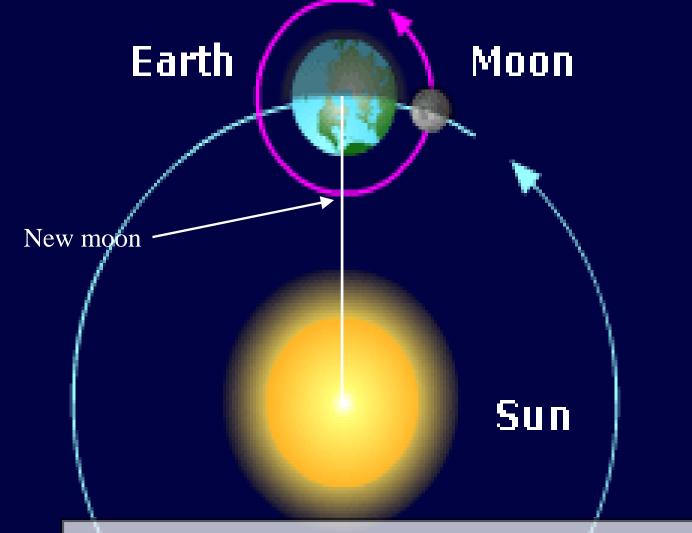
Aristarchus already computed that the radius of the Moon was 1/180 of the distance to the Moon.

He also knew that during a solar eclipse, the Moon covered the Sun almost perfectly.

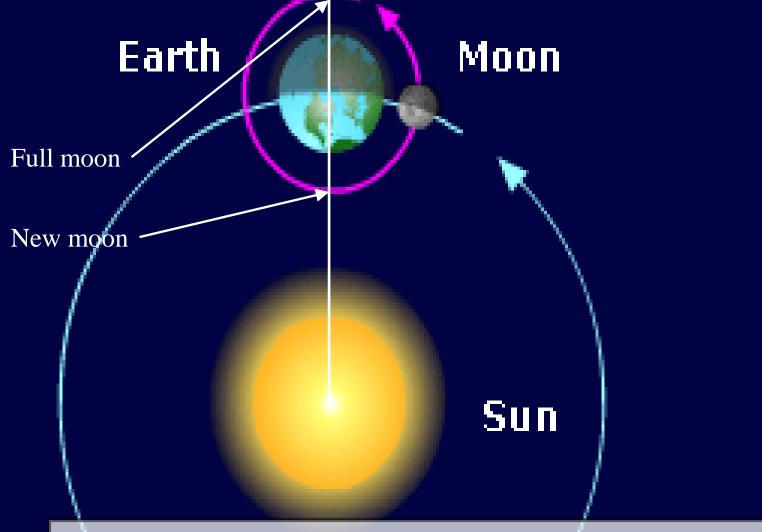
Using similar triangles, he concluded that the radius of the Sun was also 1/180 of the distance to the Sun.

So his next task was to compute the distance to the Sun.

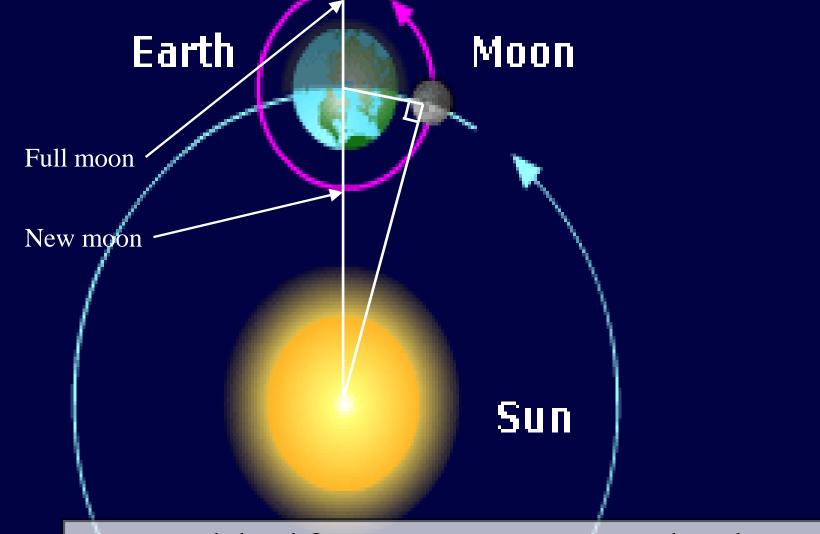
For this, he turned to the Moon again for help.



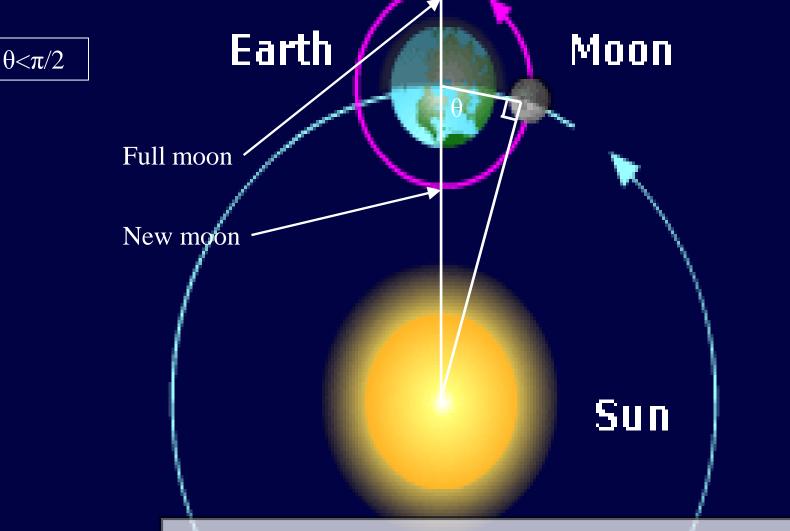
He knew that new Moons occurred when the Moon was between the Earth and Sun...



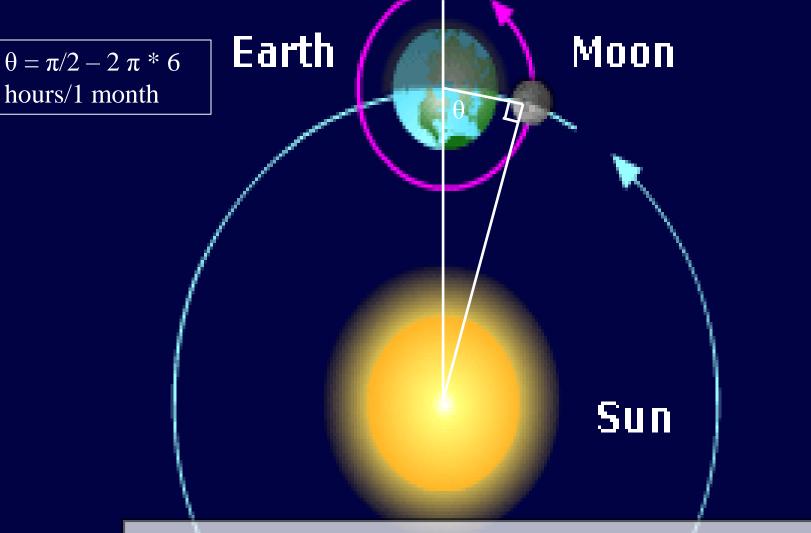
.. full Moons occurred when the Moon was directly opposite the Sun...



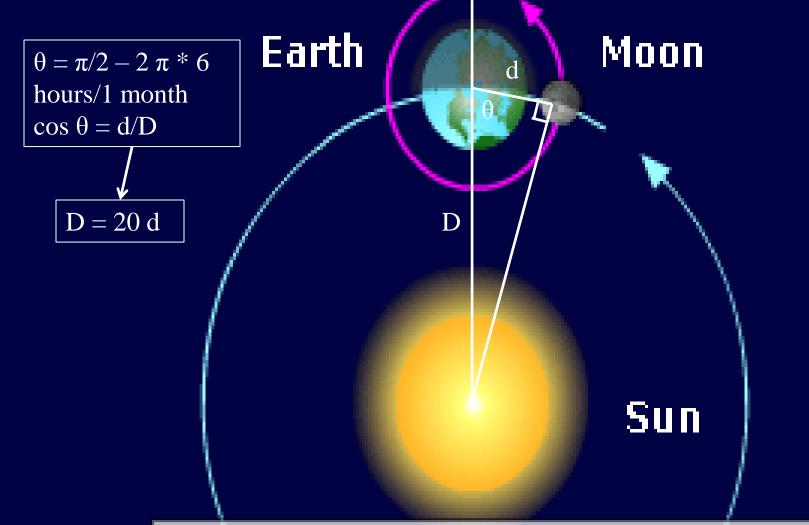
... and half Moons occurred when the Moon made a right angle between Earth and Sun.



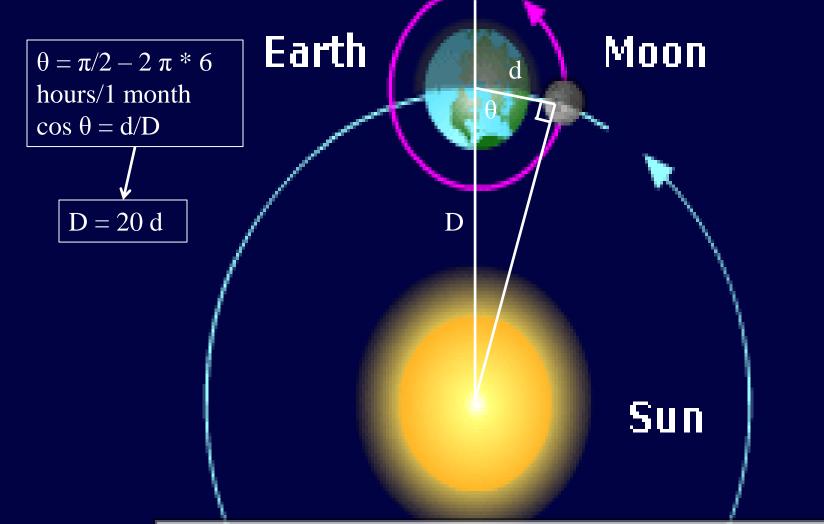
This implies that half Moons occur slightly closer to new Moons than to full Moons.



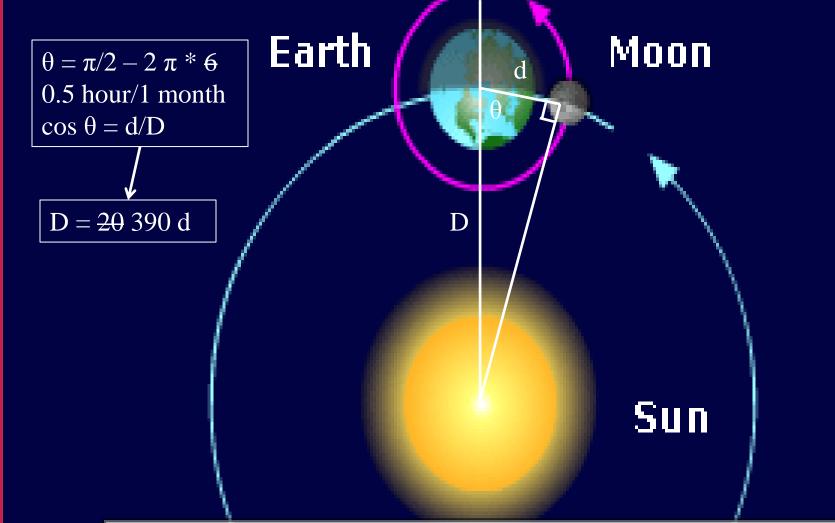
Aristarchus thought that half Moons occurred 6 hours before the midpoint of a new and full Moon.



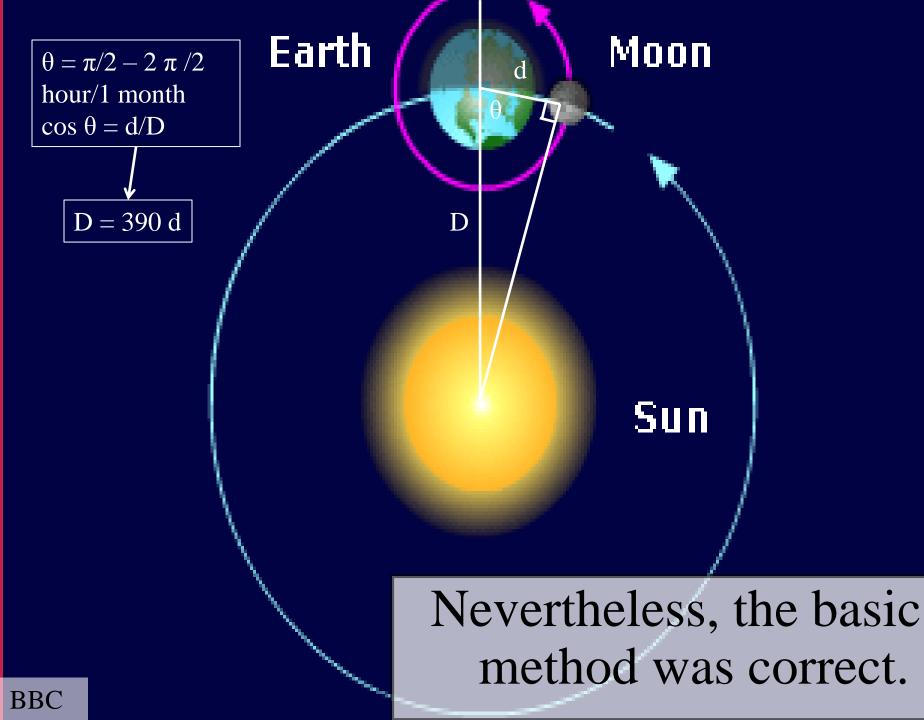
From this and trigonometry, he concluded that the Sun was 20 times further away than the Moon.

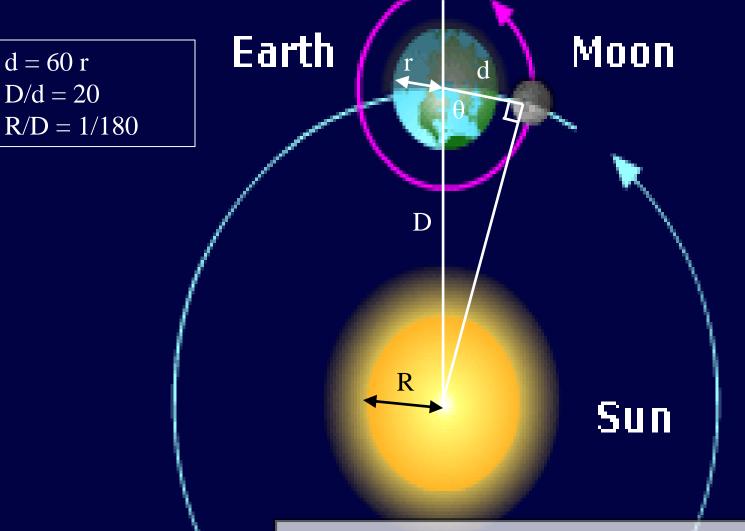


Unfortunately, with ancient Greek technology it was hard to time a new Moon perfectly.

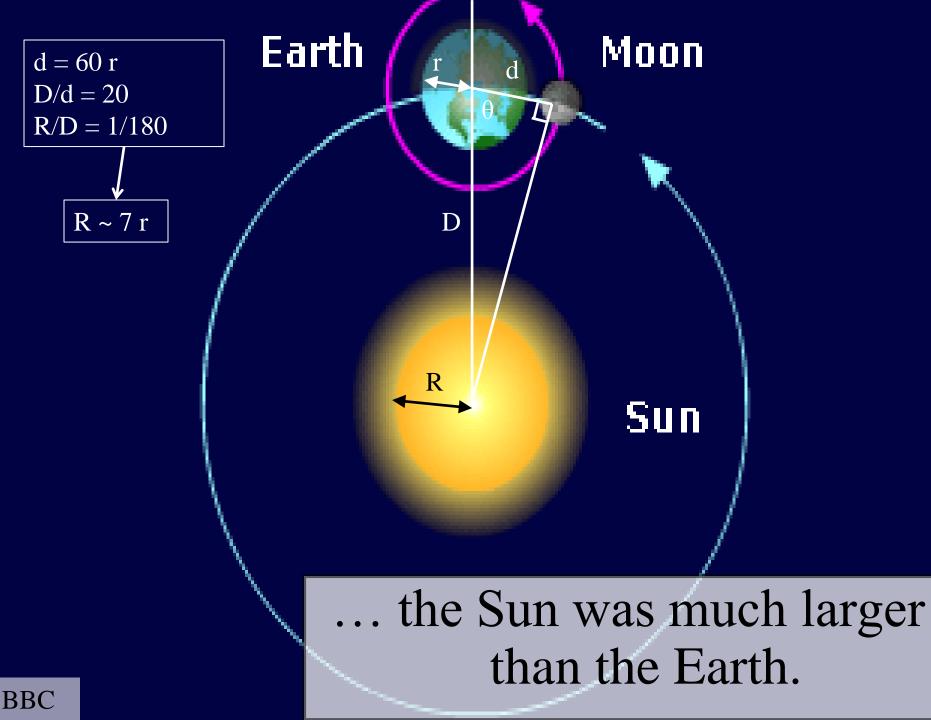


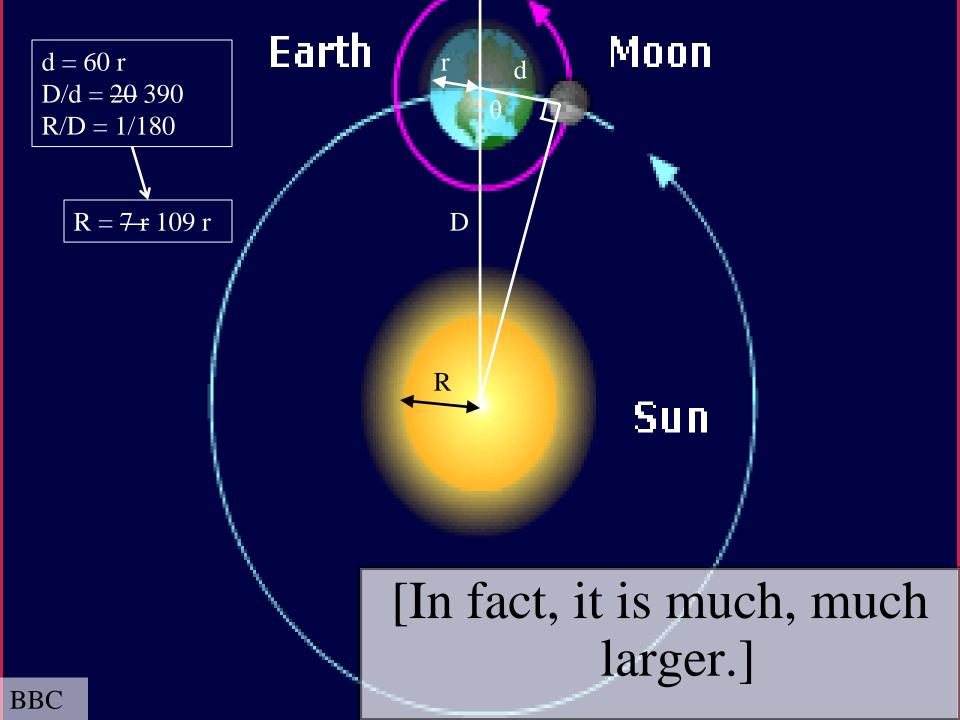
The true time discrepancy is ½ hour (not 6 hours), and the Sun is 390 times further away (not 20 times).





And Aristarchus' computations led him to an important conclusion...





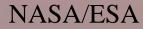
He then concluded it was absurd to think the Sun went around the Earth...



> ... and was the first to propose the heliocentric model that the Earth went around the Sun.



[1700 years later, Copernicus would credit Aristarchus for this idea.]



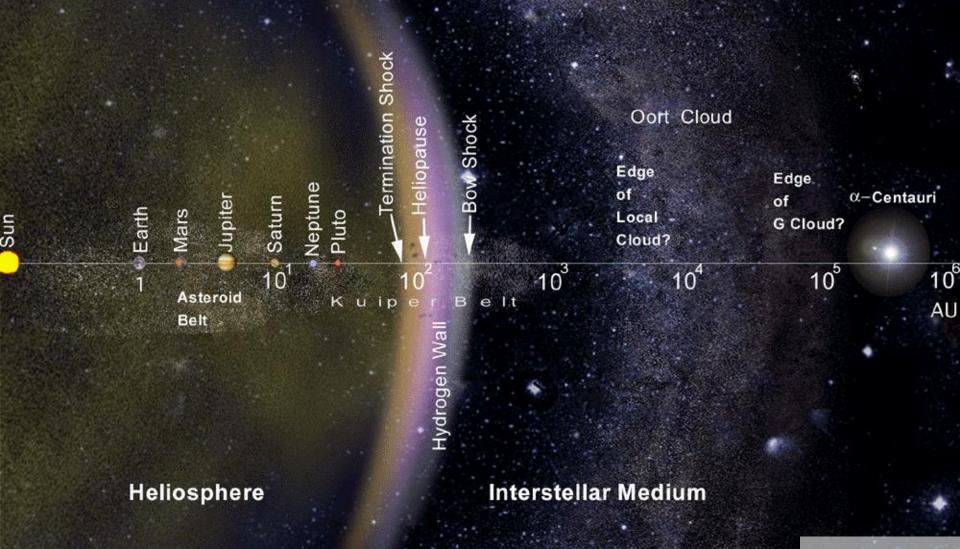
Ironically, Aristarchus' theory was not accepted by the other ancient Greeks...



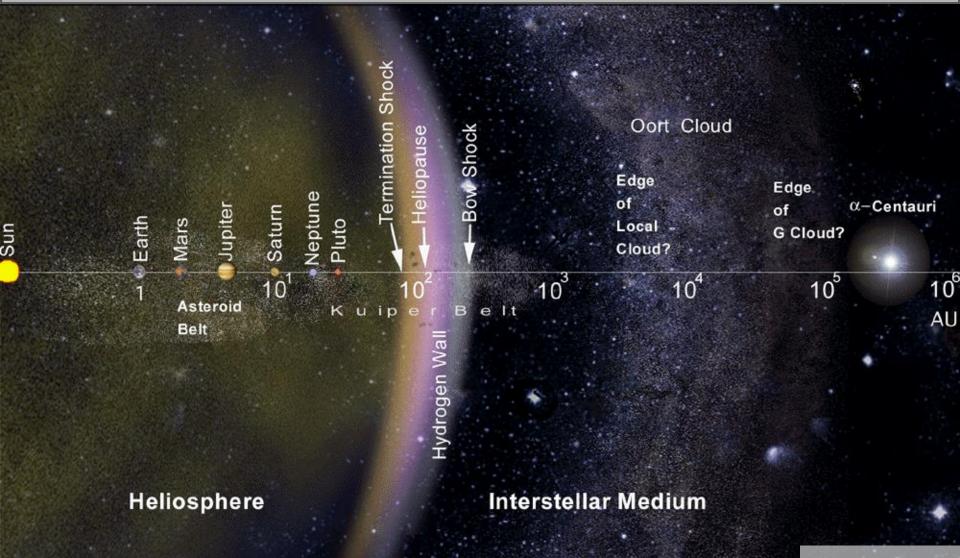
... but we'll explain why later.



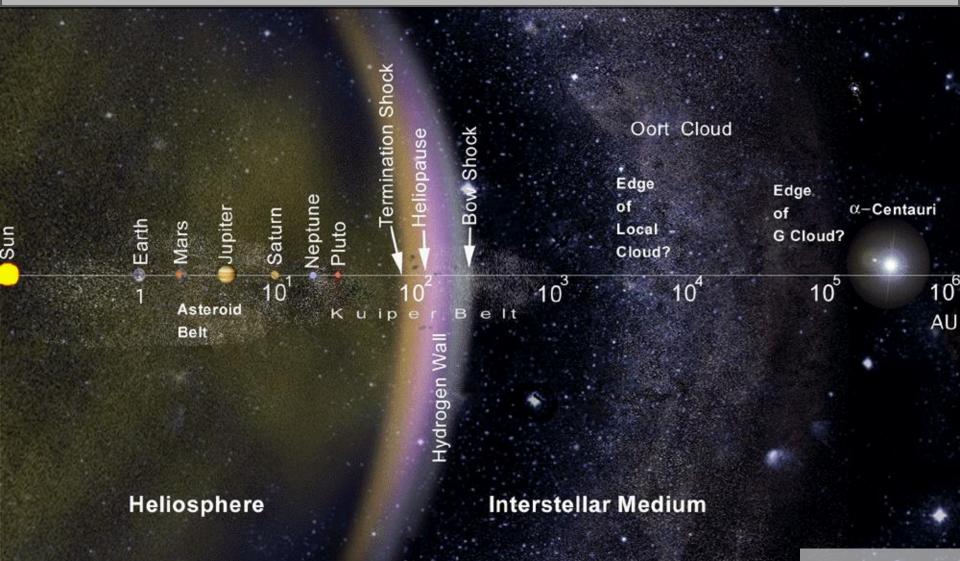
The distance from the Earth to the Sun is known as the Astronomical Unit (AU).



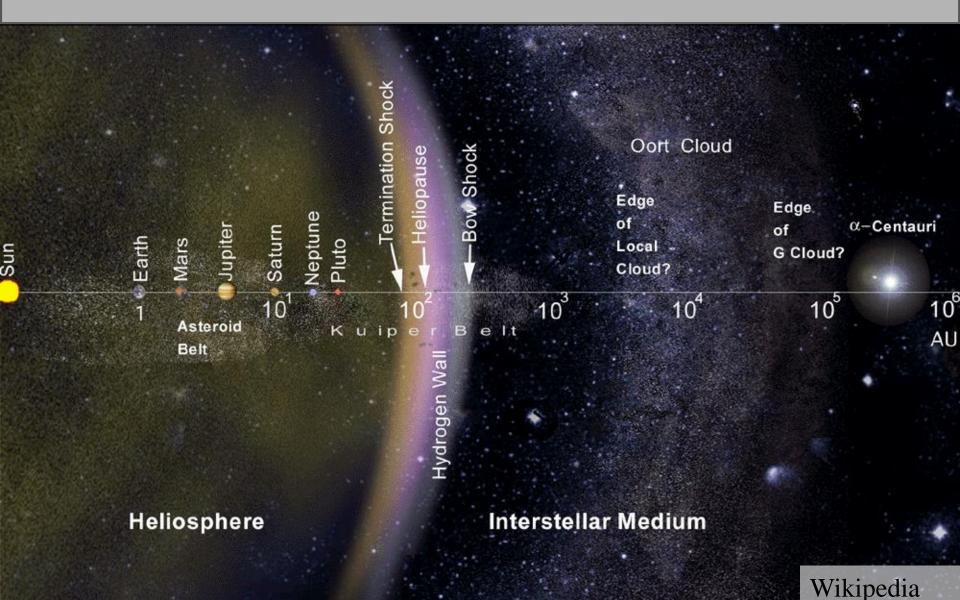
It is an extremely important rung in the cosmic distance ladder.



Aristarchus' original estimate of the AU was inaccurate...



... but we'll see much more accurate ways to measure the AU later on.



4th rung: the planets

The ancient astrologers knew that all the planets lay on a plane (the ecliptic), because they only moved through the Zodiac.

But this still left many questions unanswered:



- How far away are the planets (e.g. Mars)?
- What are their orbits?
- How long does it take to complete an orbit?

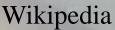


Ptolemy (90-168 CE) attempted to answer these questions, but obtained highly inaccurate answers...



... because he was working with a geocentric model rather than a heliocentric one.

The first person to obtain accurate answers was Nicolaus Copernicus (1473-1543).



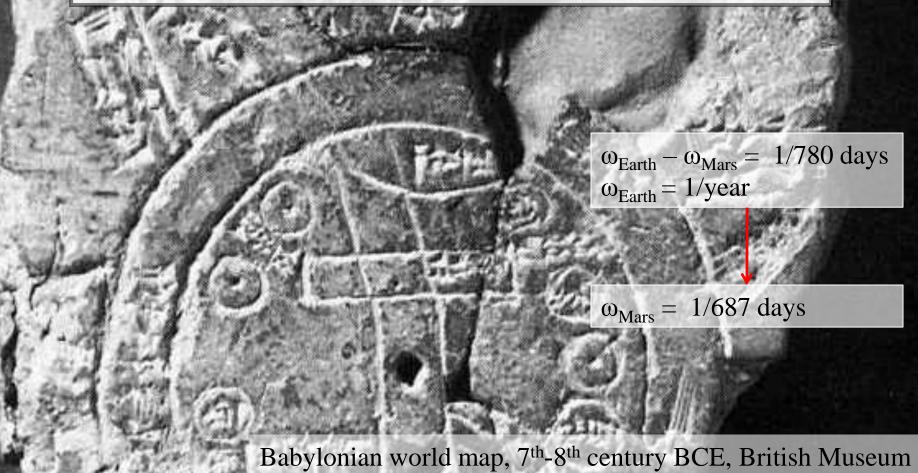
Copernicus started with the records of the ancient Babylonians, who knew that the apparent motion of Mars (say) repeated itself every 780 days (the synodic period of Mars).

 $\omega_{\text{Earth}} - \omega_{\text{Mars}} = 1/780 \text{ days}$

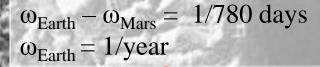
Using the heliocentric model, he also knew that the Earth went around the Sun once a year.

> $\omega_{Earth} - \omega_{Mars} = 1/780 \text{ days}$ $\omega_{Earth} = 1/\text{year}$

Subtracting the implied angular velocities, he found that Mars went around the Sun every 687 days (the sidereal period of Mars).



Assuming circular orbits, and using measurements of the location of Mars in the Zodiac at various dates...



 $\omega_{\text{Mars}} = 1/687 \text{ days}$

...Copernicus also computed the distance of Mars from the Sun to be 1.5 AU.

 $\omega_{Earth} - \omega_{Mars} = 1/780 \text{ days}$ $\omega_{Earth} = 1/\text{year}$

 $\omega_{\text{Mars}} = 1/687 \text{ days}$

Both of these measurements are accurate to two decimal places.

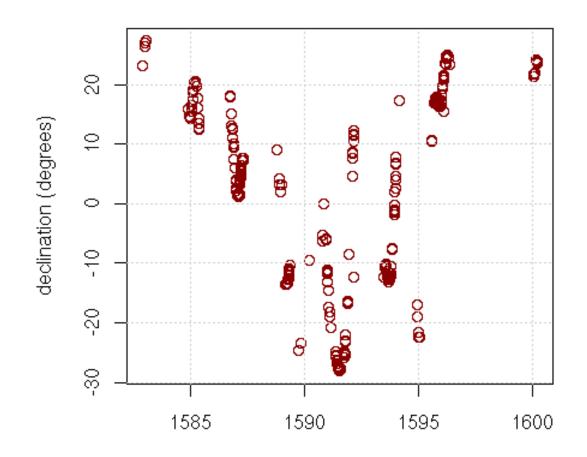
$$\begin{split} &\omega_{Earth}-\omega_{Mars}=~1/780~days\\ &\omega_{Earth}=1/year \end{split}$$

 $\omega_{\text{Mars}} = 1/687 \text{ days}$

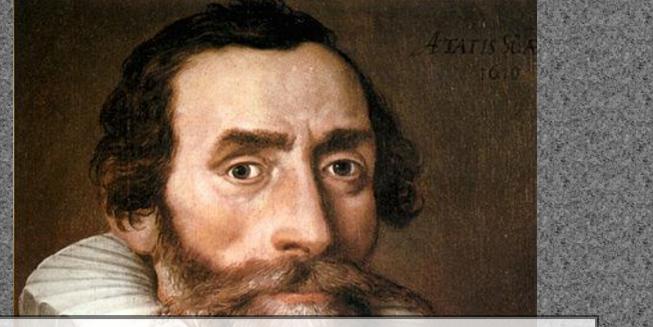
Tycho Brahe (1546-1601) made extremely detailed and long-term measurements of the position of Mars and other planets.

Unfortunately, his data deviated slightly from the predictions of the Copernican model.

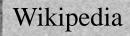
Tycho Brahe's Mars Observations

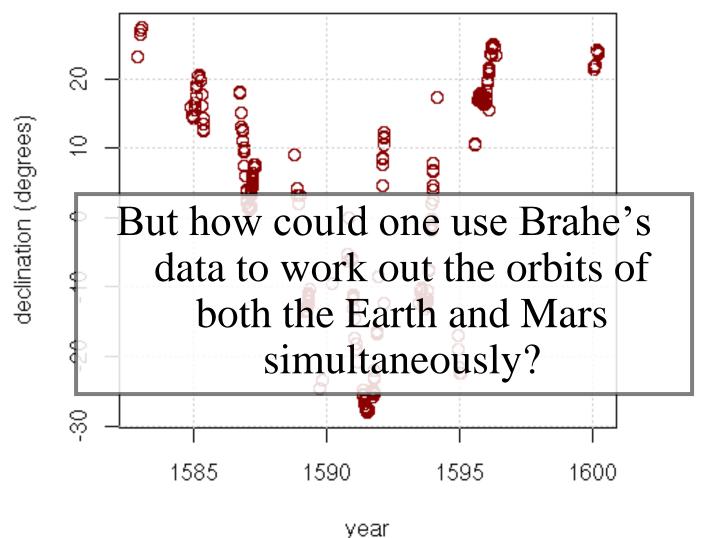


year source: Tychonis Brahe Dani Opera Omnia

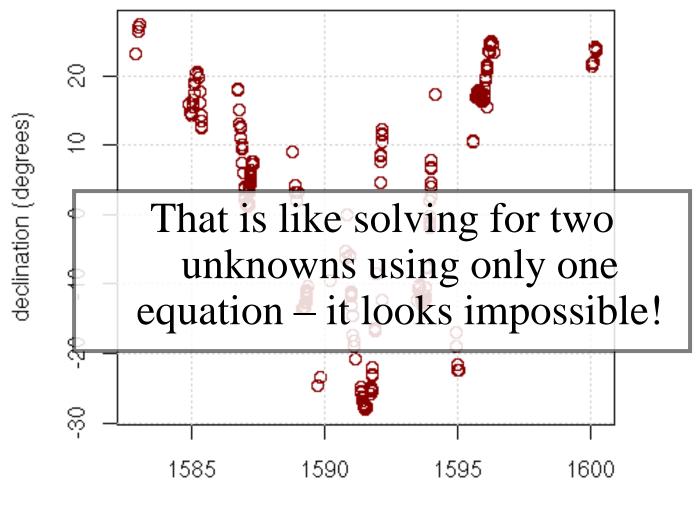


Johannes Kepler (1571-1630) reasoned that this was because the orbits of the Earth and Mars were not quite circular.

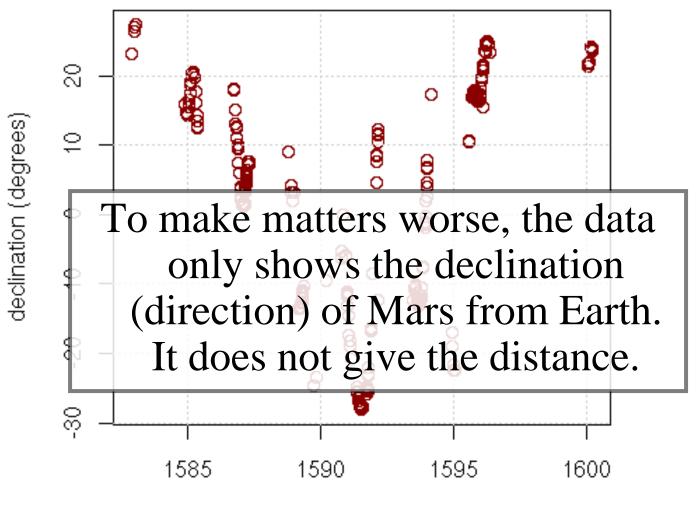




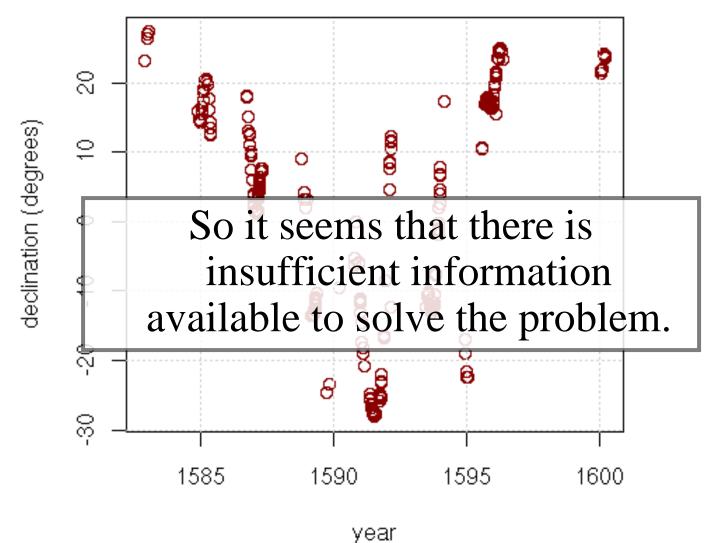
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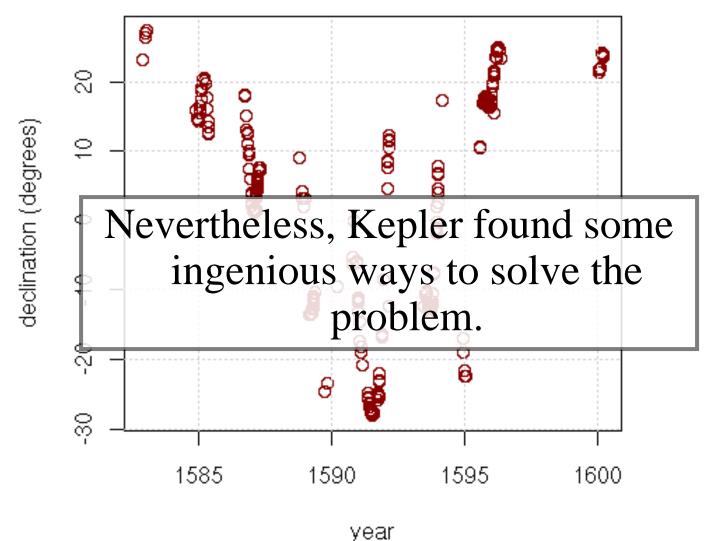
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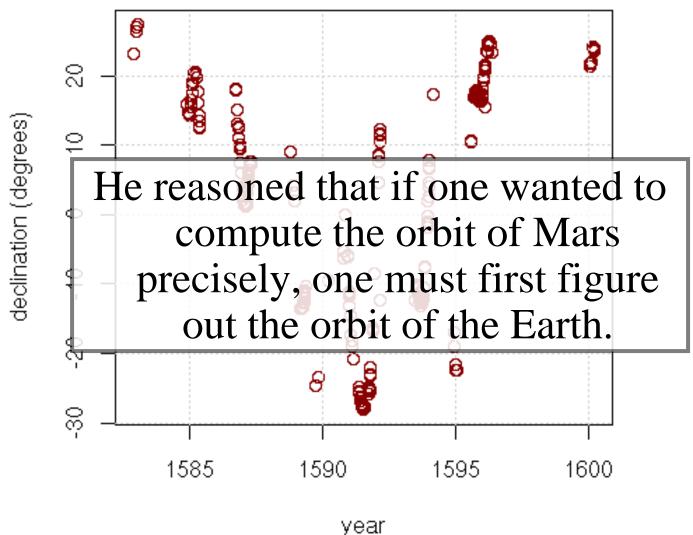
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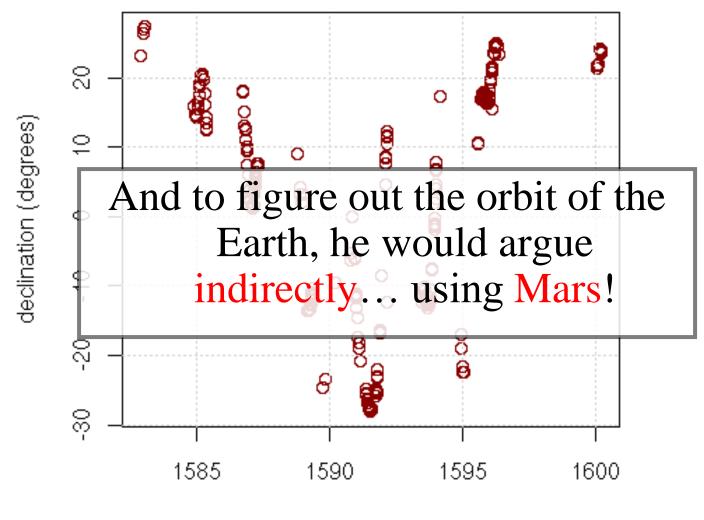
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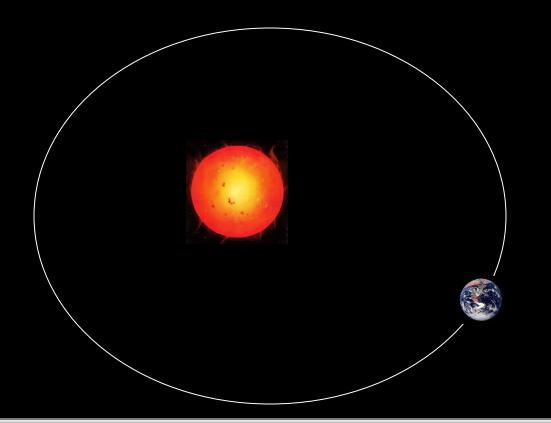


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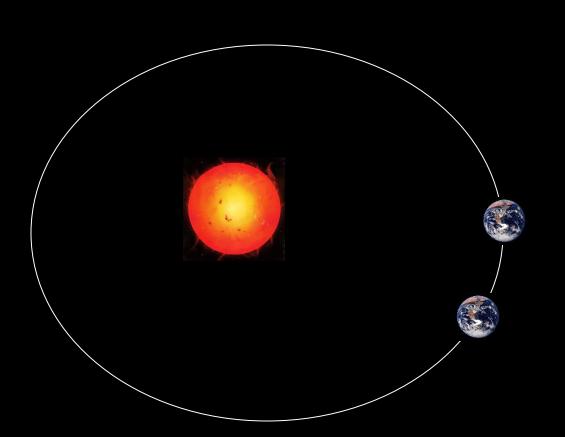


year source: Tychonis Brahe Dani Opera Omnia

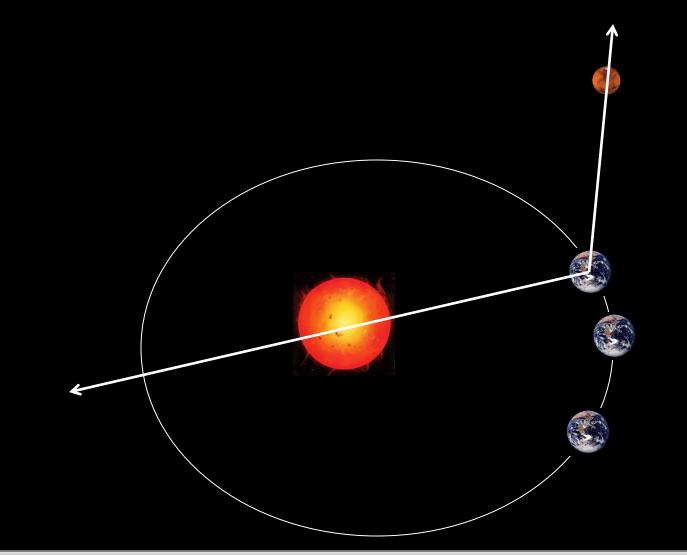




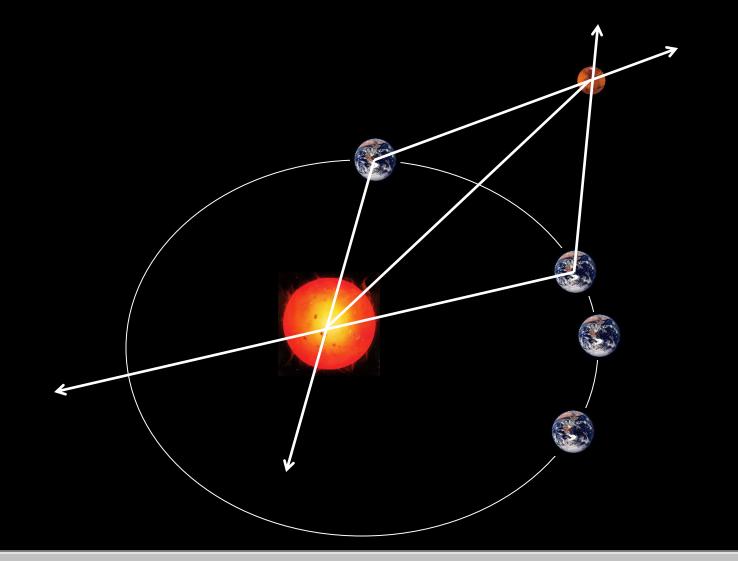
To explain how this works, let's first suppose that Mars is fixed, rather than orbiting the Sun.



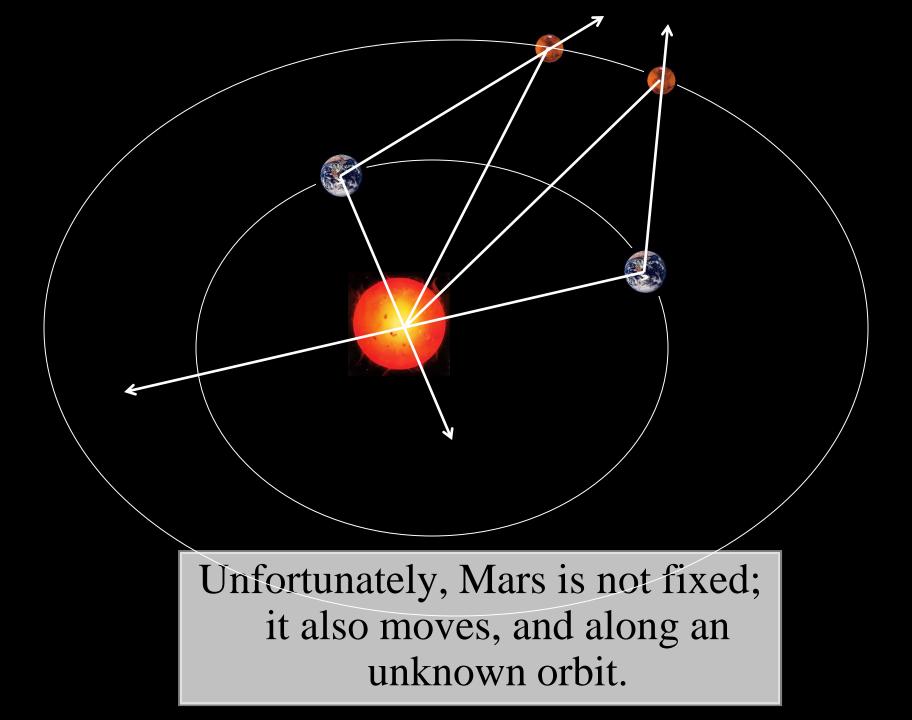
But the Earth is moving in an unknown orbit.



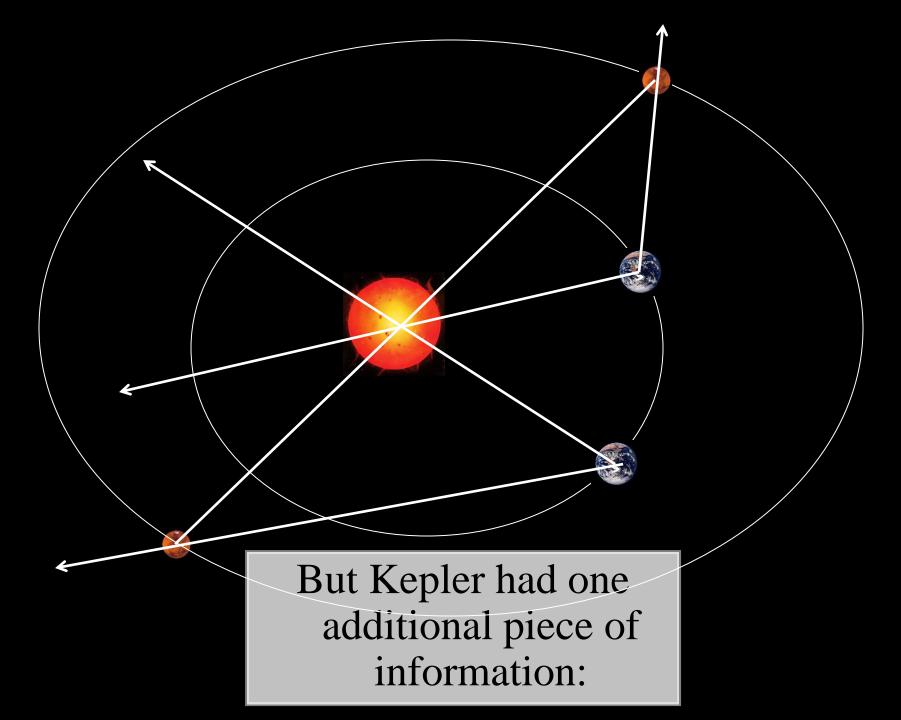
At any given time, one can measure the position of the Sun and Mars from Earth, with respect to the fixed stars (the Zodiac).

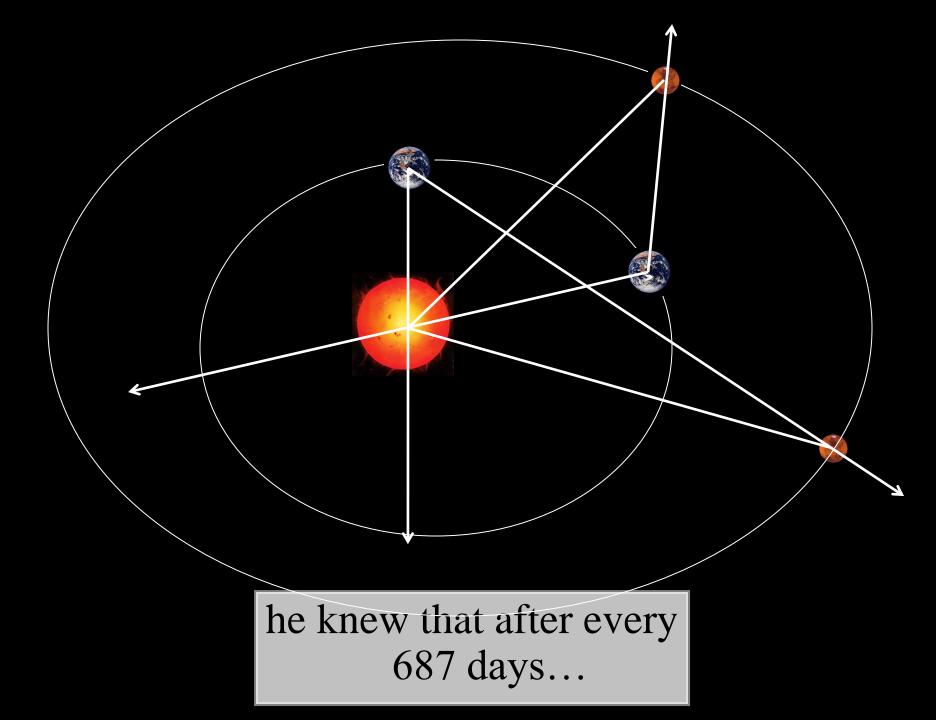


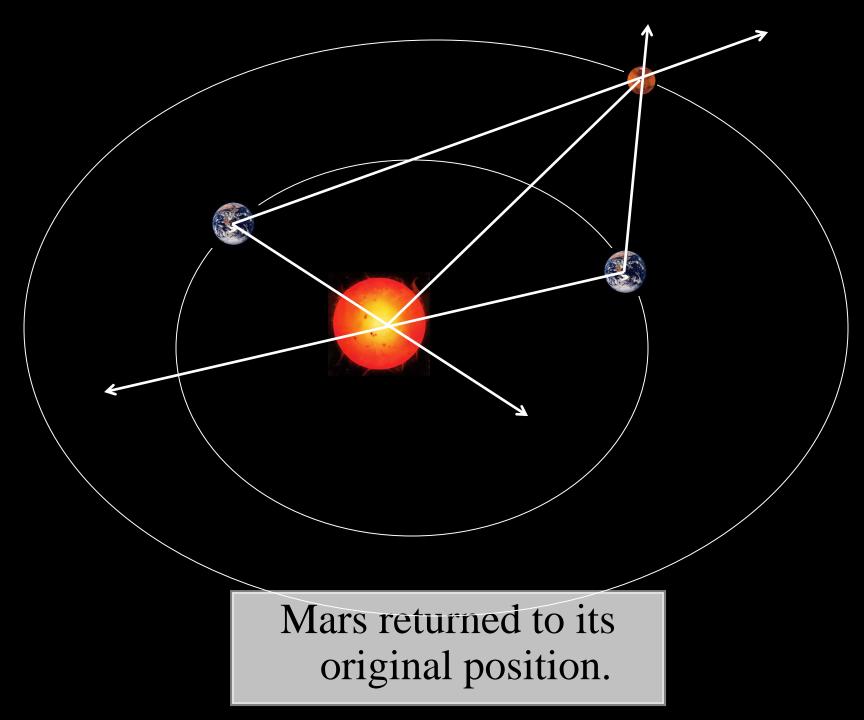
Assuming that the Sun and Mars are fixed, one can then triangulate to determine the position of the Earth relative to the Sun and Mars.

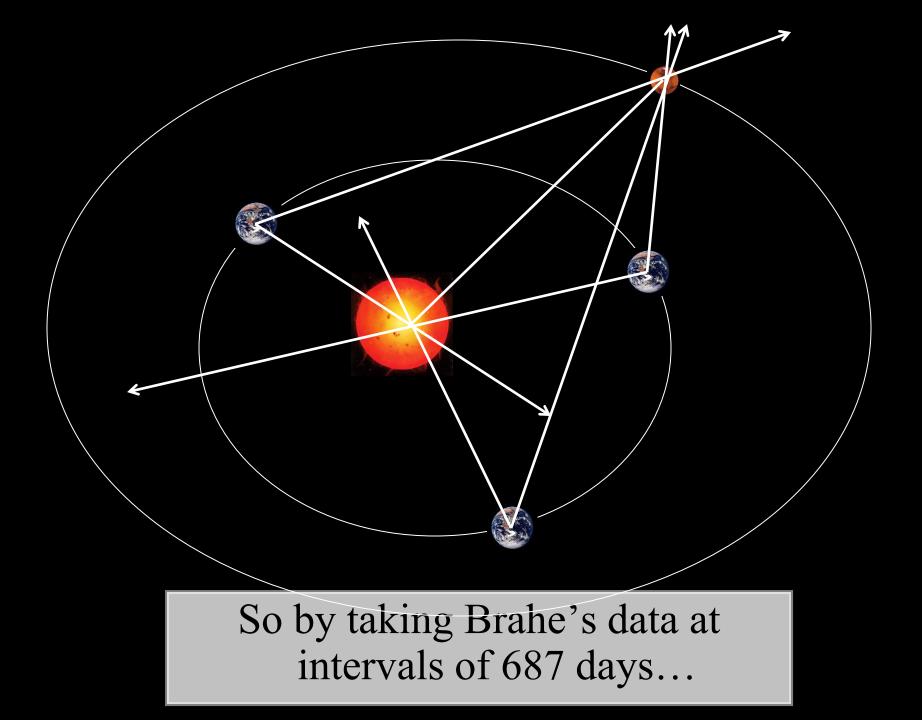


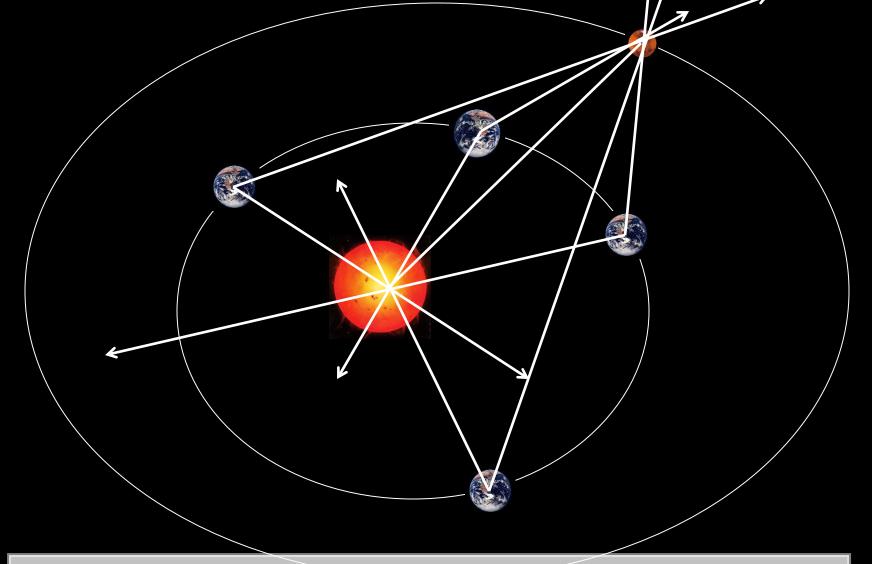
So it appears that triangulation does not work.



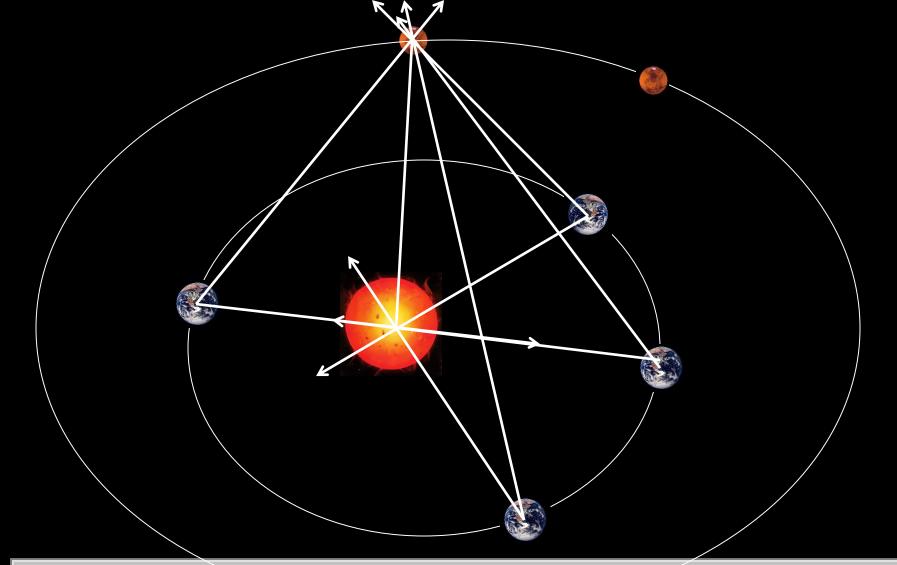








... Kepler could triangulate and compute Earth's orbit relative to any position of Mars.



Once Earth's orbit was known, it could be used to compute more positions of Mars by taking other sequences of data separated by 687 days...

... which allows one to compute the orbit of Mars.

Using the data for Mars and other planets,Kepler formulated his three laws of planetary motion.

Kepler's laws of planetary motion

- 1. Planets orbit in ellipses, with the Sun as one of the foci.
- 2. A planet sweeps out equal areas in equal times.
- 3. The square of the period of an orbit is

NASA

proportional to the cube of its semi-major axis.

This helped Isaac Newton (1643-1727) in formulating and confirming his law of gravity.

Newton's law of universal gravitation Any pair of masses attract by a force proportional to the masses, and inversely proportional to the square of the distance.

 $|F| = G m_1 m_2 / r^2$

Kepler's methods allowed for very precise measurements of planetary distances in terms of the AU.

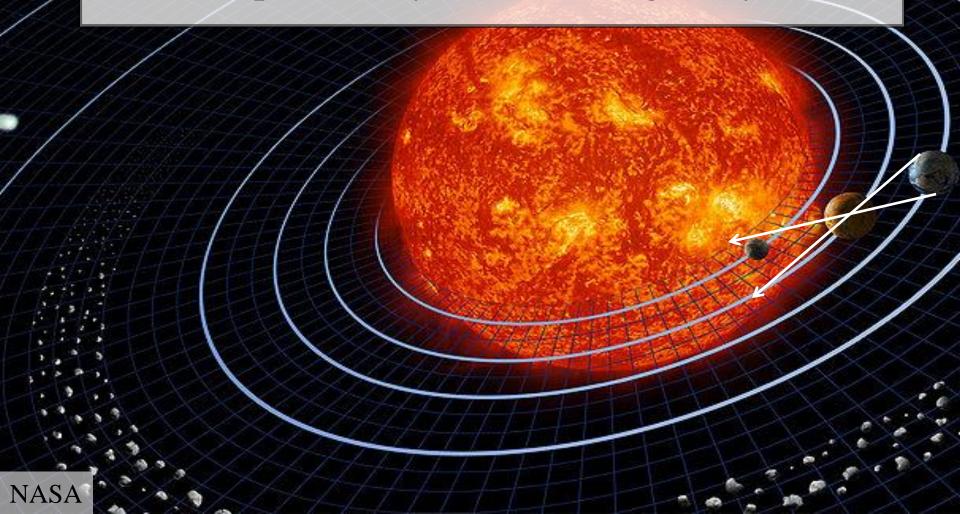
Mercury: 0.307-0.466 AU Venus: 0.718-0.728 AU Earth: 0.98-1.1 AU Mars: 1.36-1.66 AU Jupiter: 4.95-5.46 AU Saturn: 9.05-10.12 AU Uranus: 18.4-20.1 AU Neptune: 29.8-30.4 AU Conversely, if one had an alternate means to compute distances to planets, this would give a measurement of the AU. One way to measure such distances is by parallax – measuring the same object from two different locations on the Earth.

NASA

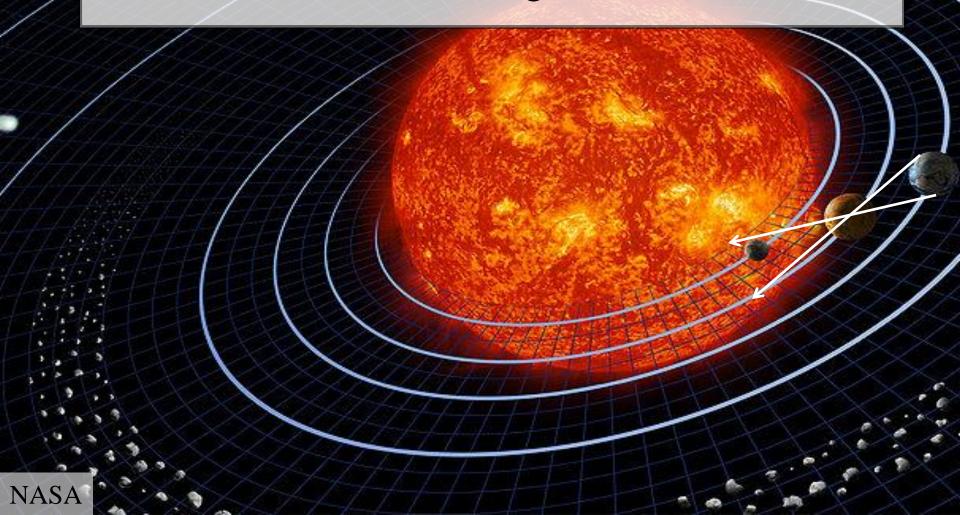
By measuring the parallax of the transit of Venus across the Sun simultaneously in several locations (including James Cook's voyage!), the AU was computed reasonably accurately in the 18th century^{*}. With modern technology such as radar and interplanetary satellites, the AU and the planetary orbits have now been computed to extremely high precision.

1 AU = 149,597,871 km = 92,955,807 mi

Incidentally, such precise measurements of Mercury revealed a precession that was not explained by Newtonian gravity...



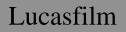
..., and was one of the first experimental verifications of general relativity (which is needed in later rungs of the ladder).



5th rung: the speed of light



Technically, the speed of light, *c*, is not a distance.

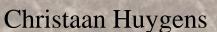


However, one needs to know it in order to ascend higher rungs of the distance ladder.



The first accurate measurements of *c* were by Ole Rømer (1644-1710) and Christiaan Huygens (1629-1695).

Their method was indirect... and used a moon of Jupiter, namely Io.



Io has the shortest orbit of all the major moons of Jupiter. It orbits Jupiter once every 42.5 hours.

Rømer made many measurements of this orbit by timing when Io entered and exited Jupiter's shadow.

He noticed* that when Jupiter was aligned with the Earth, the orbit advanced slightly; when Jupiter was opposed, the orbit lagged.

* As Romer could not observe Io in the daytime, his actual calculations occurred when Earth made an acute angle with Jupiter.

The difference was slight; the orbit lagged by about 20 minutes when Jupiter was opposed.

Huygens reasoned that this was because of the additional distance (2AU) that the light from Jupiter had to travel.

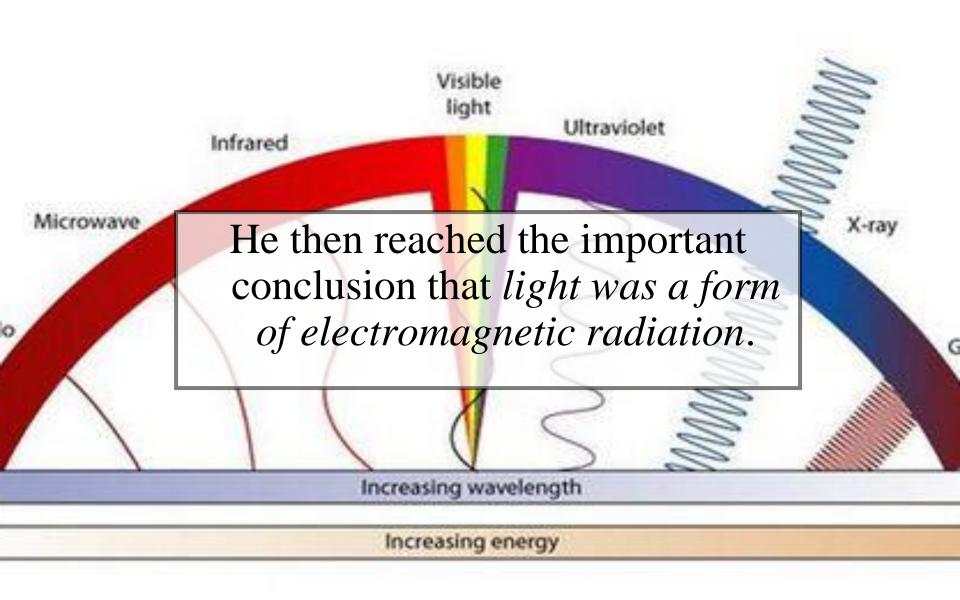
Using the best measurement of the AU available to him, he then computed the speed of light as c =220,000 km/s = 140,000 mi/s. [The truth is 299,792 km/s = 186,282 mi/s.]

This computation was important for the future development of physics.



James Clerk Maxwell (1831-1879) observed that the speed of light almost matched the speed his theory predicted for electromagnetic radiation.

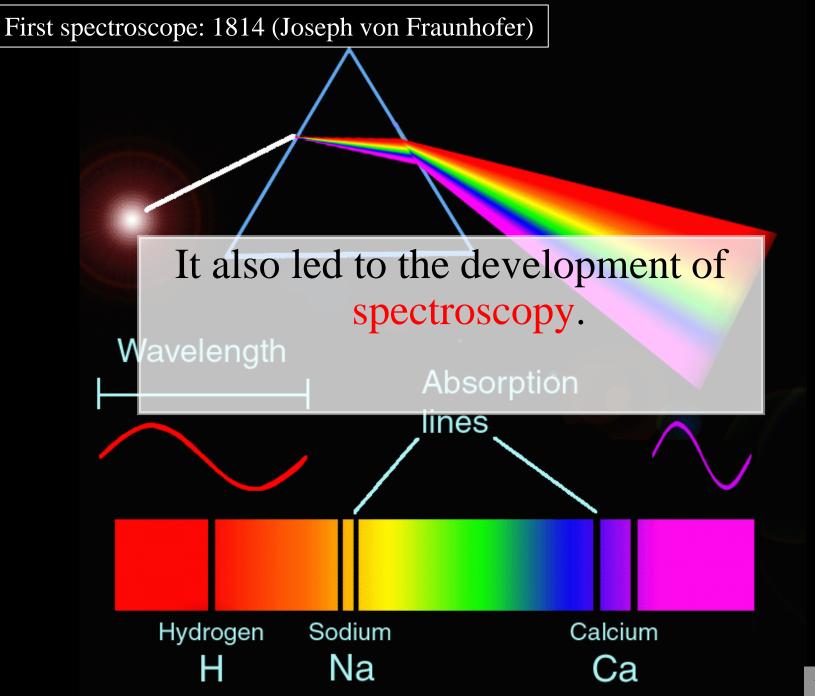
c ~ 3.0 x 10⁸ m/s $\varepsilon_0 \sim 8.9 \times 10^{-12}$ F/m $\mu_0 \sim 1.3 \times 10^{-6}$ H/m $(\varepsilon_0 \mu_0)^{-1/2} \sim 3.0 \times 10^8$ m/s



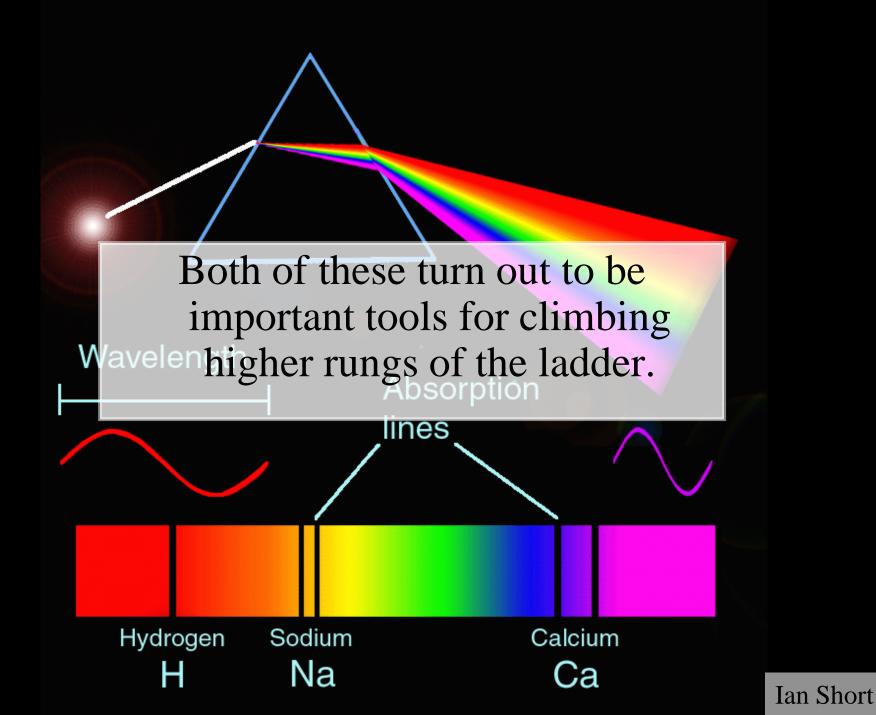
Science Learning Hub, University of Waikato, NZ

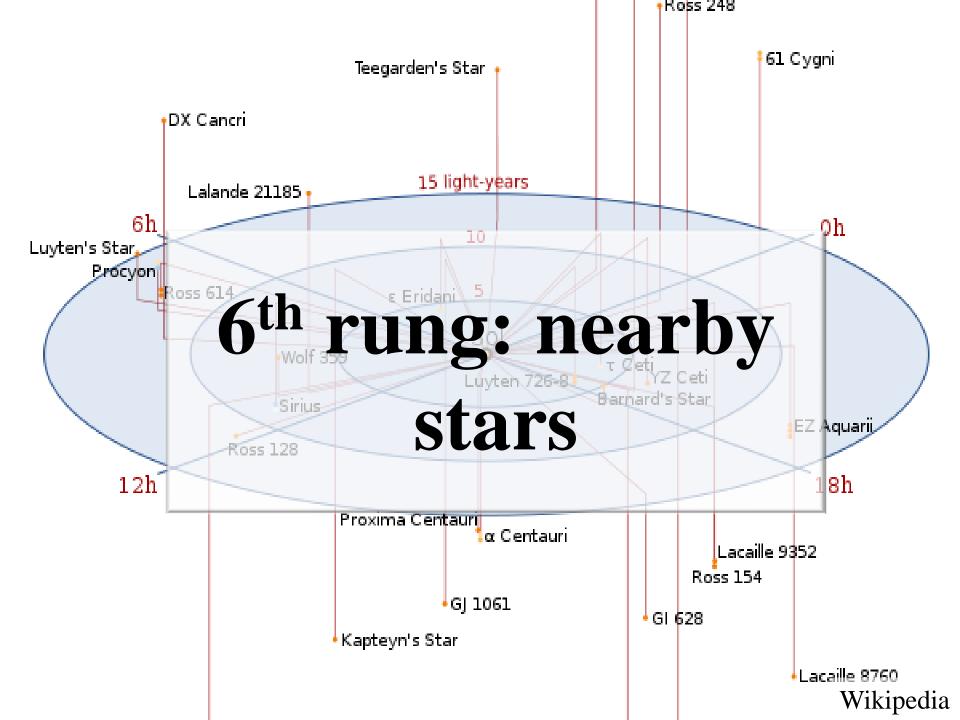
This observation was instrumental in leading to Einstein's theory of special relativity in 1905.

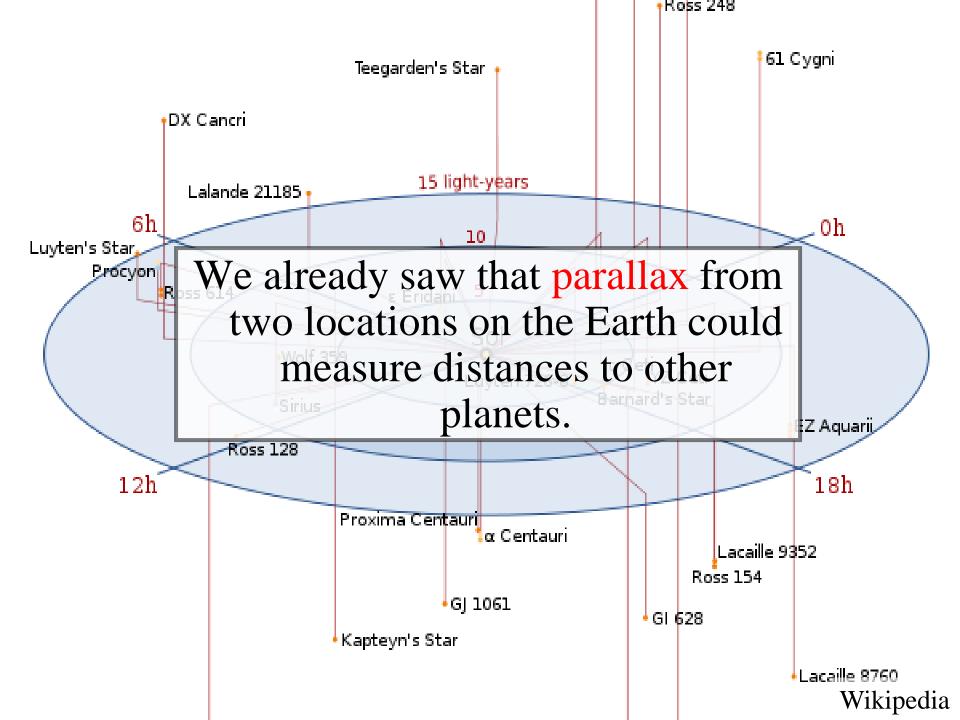
Wikipedia

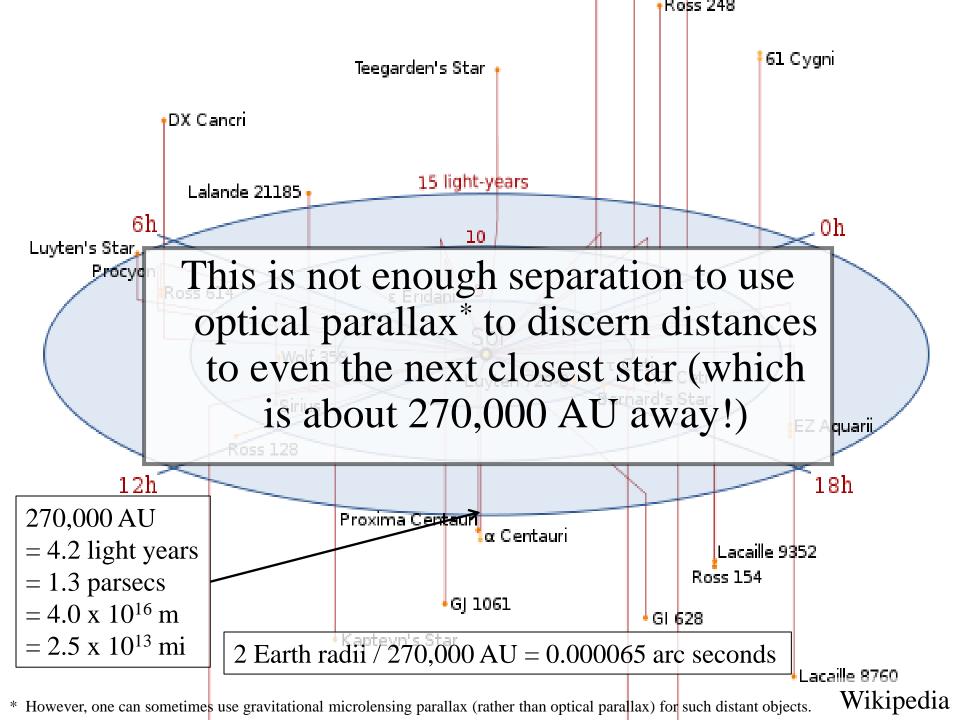


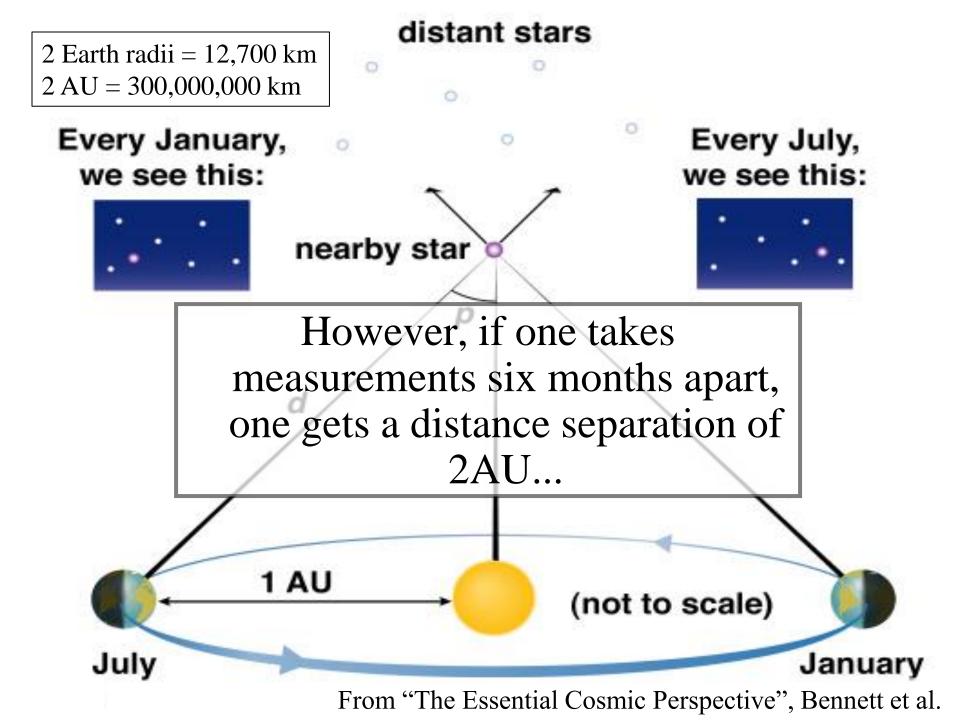
Ian Short

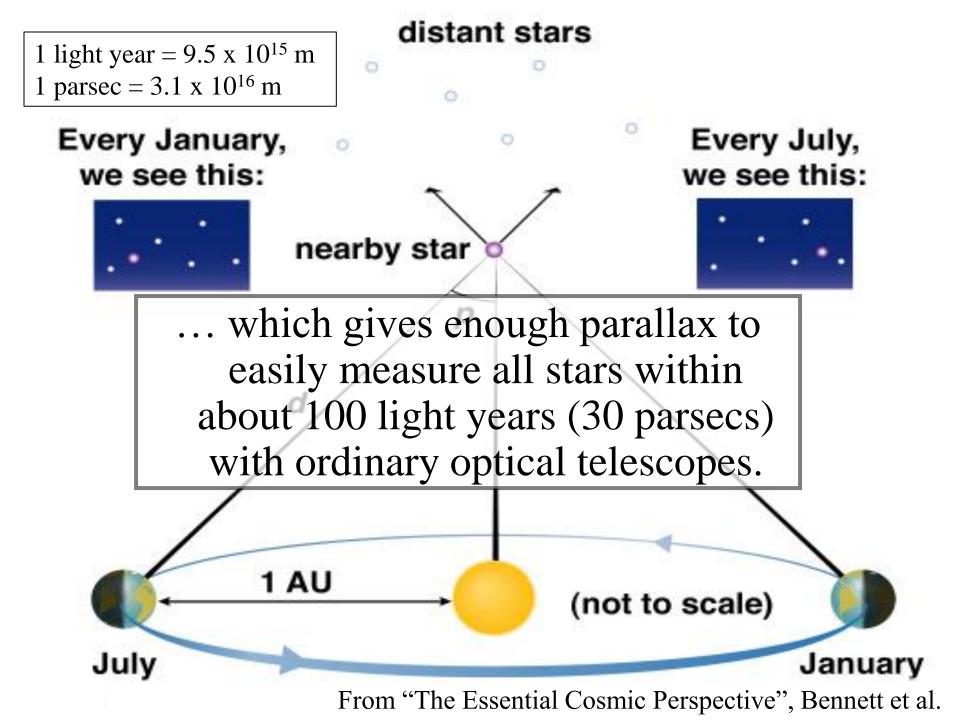


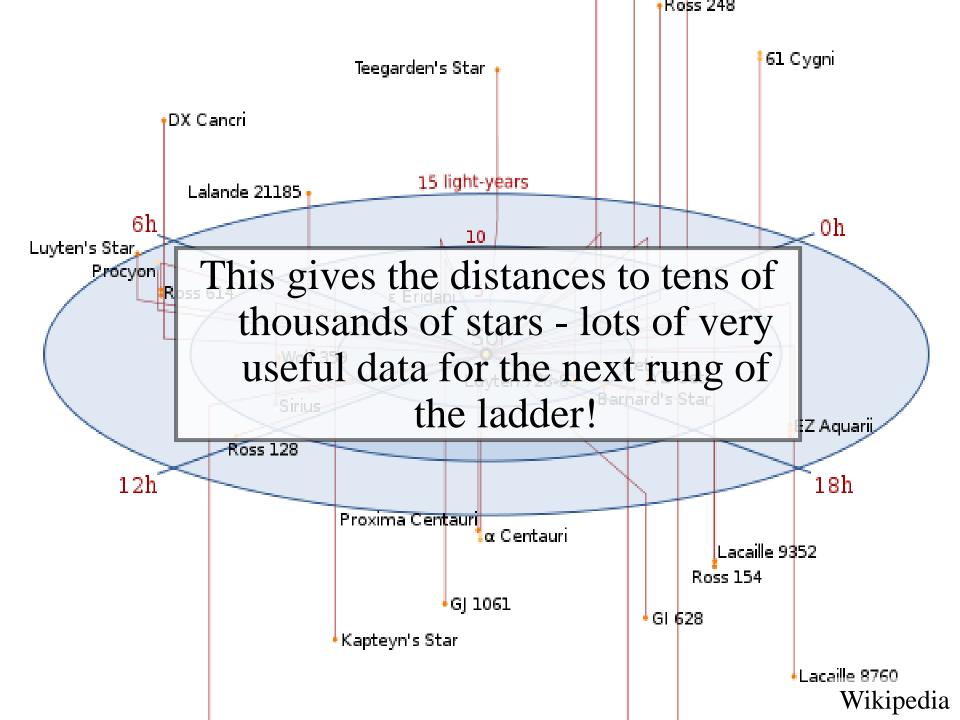




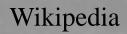




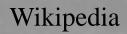




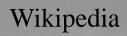
These parallax computations, which require accurate telescopy, were first done by Friedrich Bessel (1784-1846) in 1838.



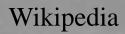
Nowadays, with modern telescopes (such as the satellite telescope Hipparcos), the parallax method can measure distances up to about 10,000 light years away.



Ironically, when Aristarchus proposed the heliocentric model, his contemporaries dismissed it, on the grounds that they did not observe any parallax effects...

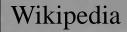


... so the heliocentric model would have implied that the stars were an absurdly large distance away.



[Which, of course, they are.]

Distance to Proxima Centauri = 40,000,000,000,000 km = 25,000,000,000,000 mi



7th rung: the Milky Way

One can use detailed observations of nearby stars to provide a means to measure distances to more distant stars. Using spectroscopy, one can measure precisely the colour of a nearby star; using photography, one can also measure its apparent brightness.

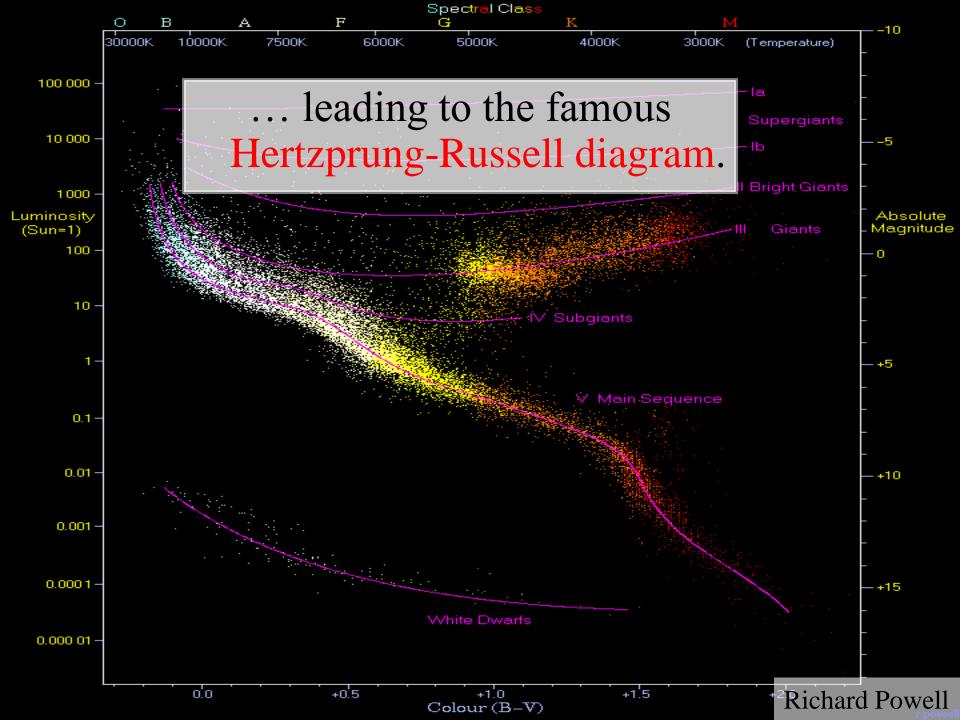
Using the apparent brightness, the distance, and inverse square law, one can compute the absolute brightness of these stars.

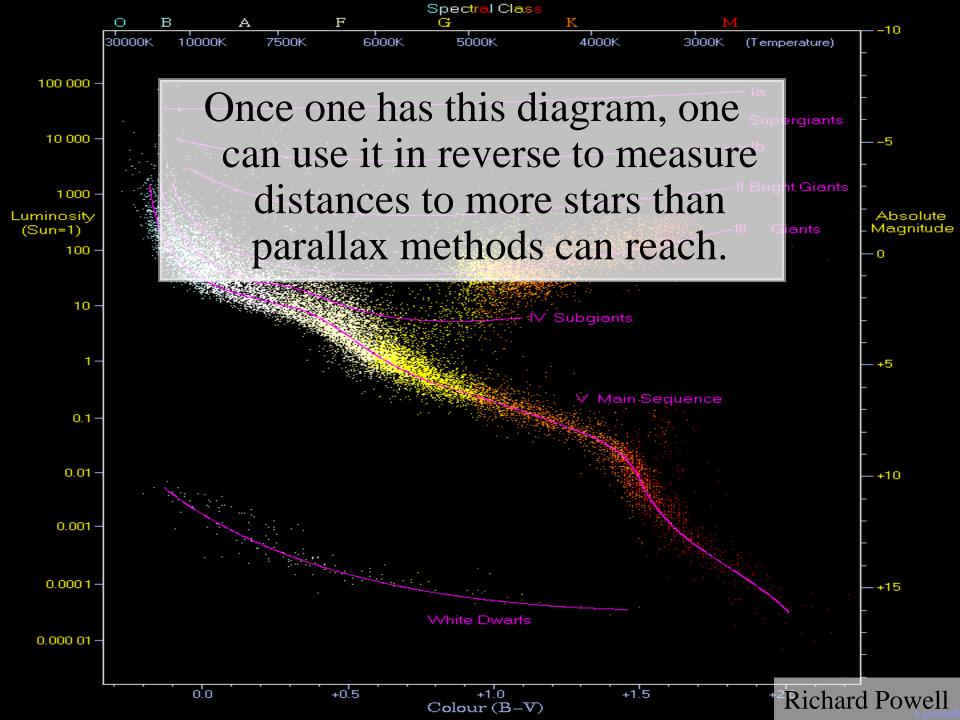
$$M = m - 5(\log_{10} D_L - 1)$$

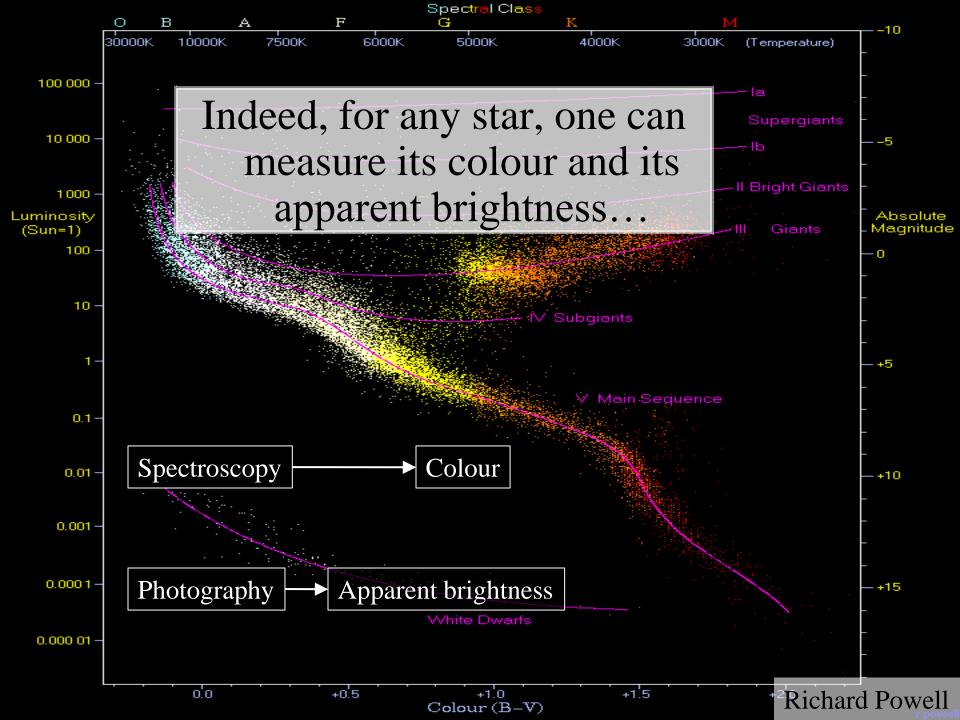
Ejnar Hertzsprung (1873-1967) and Henry Russell (1877-1957) plotted this absolute brightness against color for thousands of nearby stars in 1905-1915...

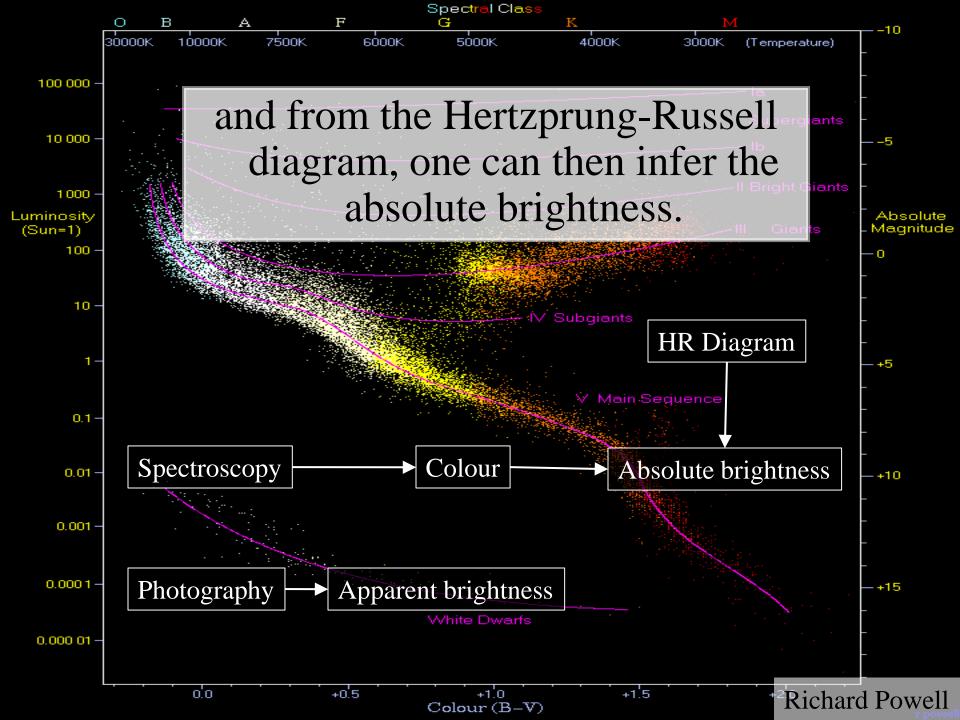
Leiden Observatory

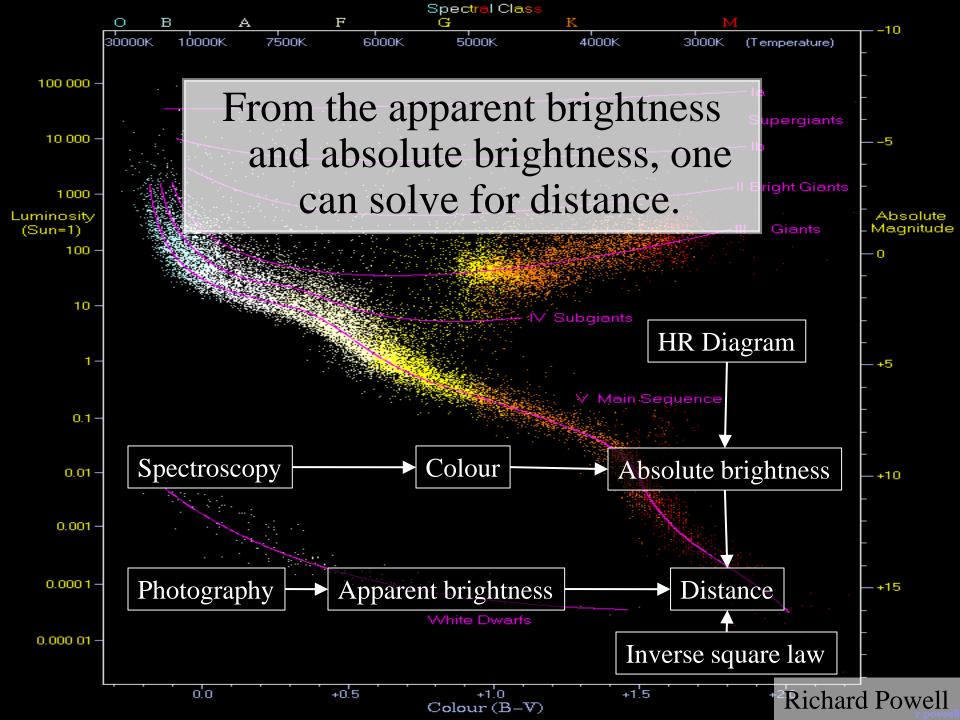
University of Chicago/Yerkes Observatory











This technique (main sequence fitting) works out to about 300,000 light years (covering the entire galaxy!)

300,000 light years = $2.8 \times 10^{21} \text{ m} = 1.8 \times 10^{18} \text{ mi}$ Diameter of Milky Way = 100,000 light years Distance to galactic center = 25,000 light years = $2.4 \times 10^{20} \text{ m} = 1.5 \times 10^{17} \text{ mi}$

Beyond this distance, the main sequence stars are too faint to be measured accurately.

8th rung: Other galaxies

Hubble deep field, NASA

Henrietta Swan Leavitt (1868-1921) observed a certain class of stars (the Cepheids) oscillated in brightness periodically.

American Institute of Physics

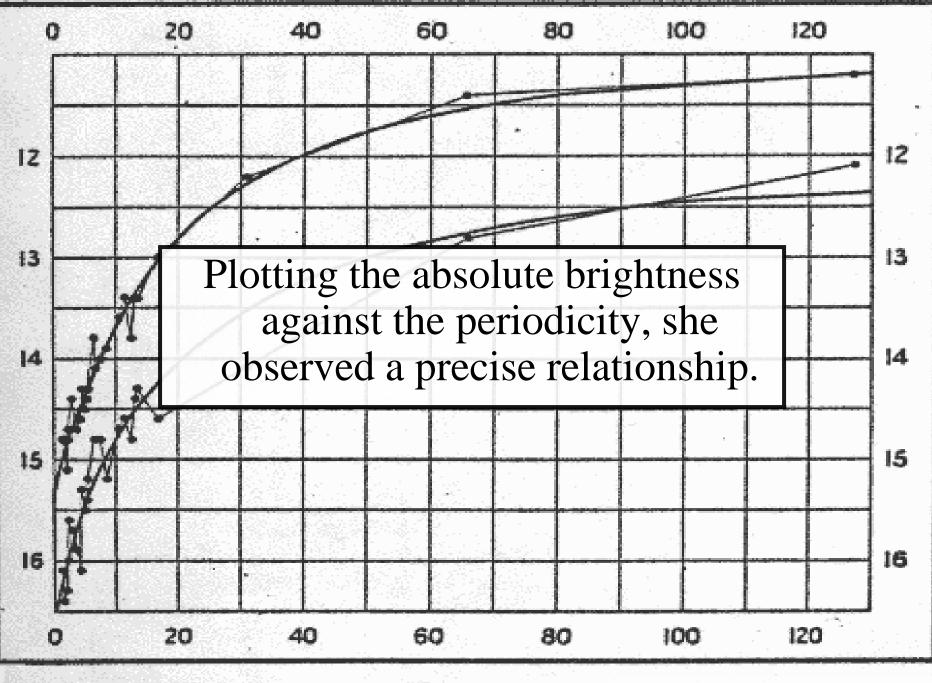


FIG. 1. Henrietta Swan Leavitt, 1912

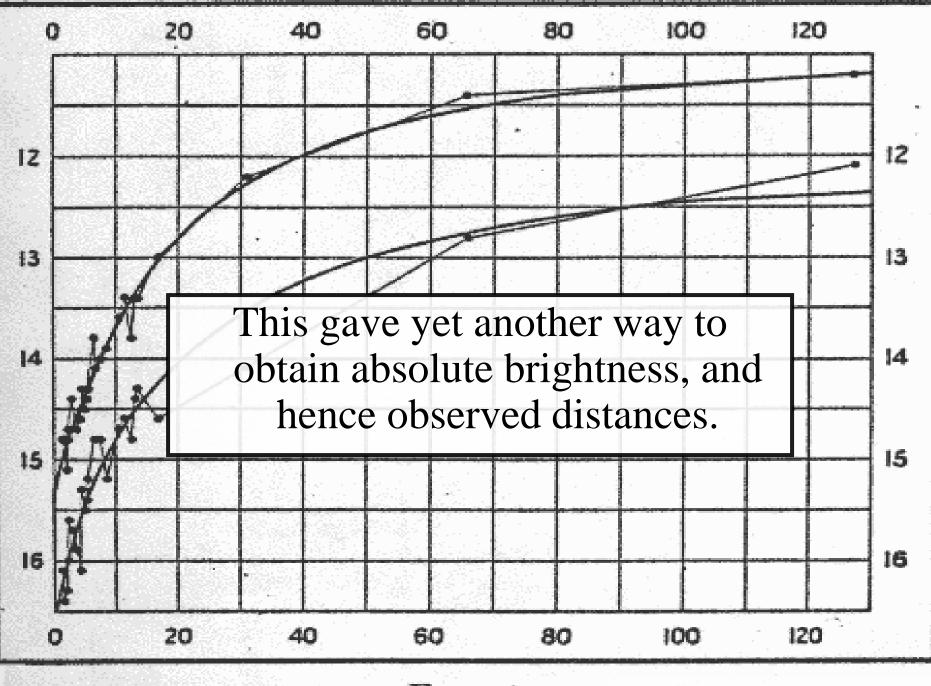
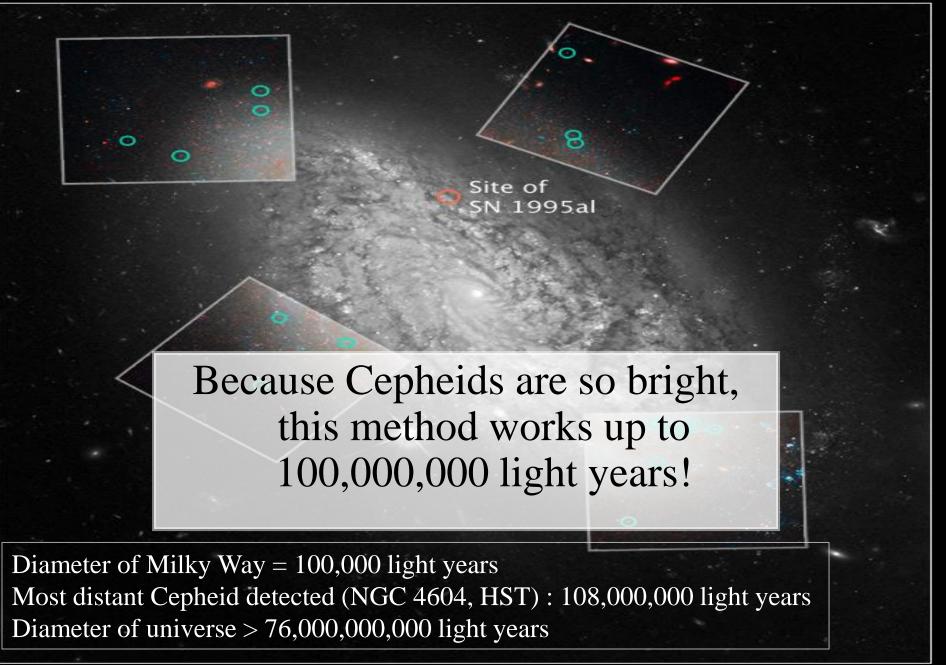


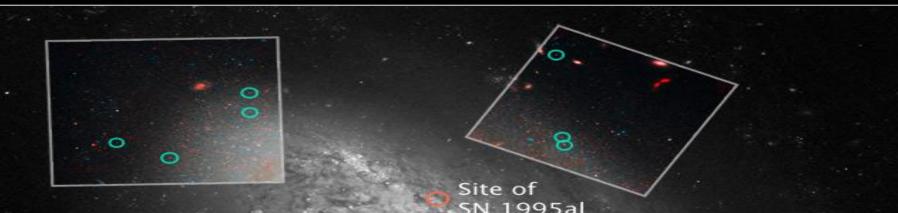
FIG. 1. Henrietta Swan Leavitt, 1912

Spiral Galaxy NGC 3021

HST • ACS/WFC • NICMOS



NASA, ESA, and A. Riess (STScl/JHU)



Most galaxies are fortunate to have at least one Cepheid in them, so we know the distances to all galaxies out to a reasonably large distance.

0

Galactic* Bulge

SS433

Norma Arm

Circinus

Local Ar

Cepheid measurements also allowed Harlow Shapley (1885-1972) to map the Milky Way, showing that the solar system was not at the centre of its own galaxy.

Cassiopeia A

rius Arm

Nebula Schematic side view of Milky Way (NASA/CXC/M. Weiss)

Sun

Crab

Diameter of Milky Way = 100,000 light years Most distant Cepheid detected (NGC 4604, HST) : 108,000,000 light years Most distant Type 1a supernova detected (1997ff) : 11,000,000,000 light years Diameter of universe > 76,000,000,000 light years

Similar methods, using supernovae instead of Cepheids, can sometimes work to even larger scales than these, and can also be used to independently confirm the Cepheid-based distance measurements.

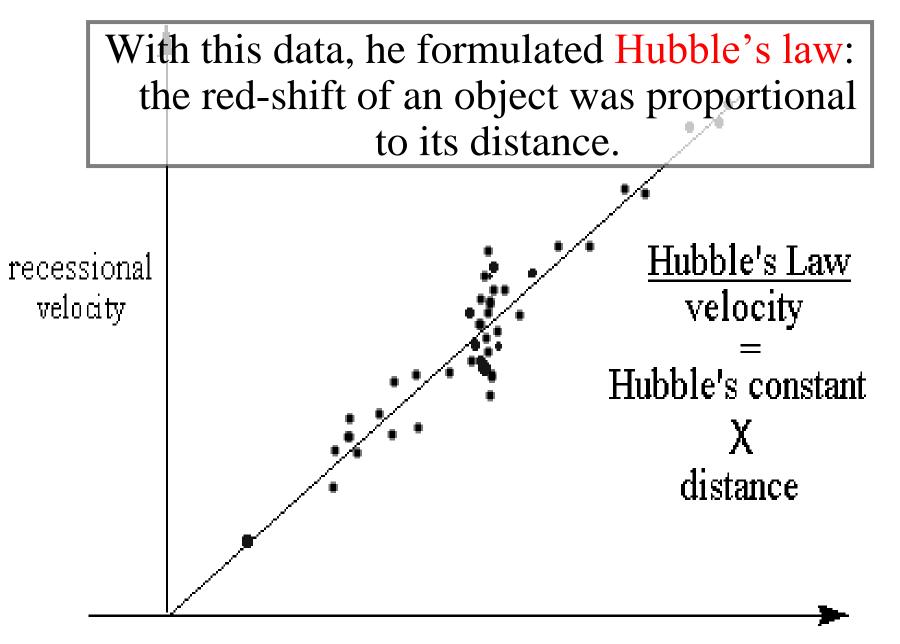
Supernova remnant, NASA, ESA, HEIC, Hubble Heritage Team

9th rung: the universe

Simulated matter distribution in universe, Greg Bryan

Edwin Hubble (1889-1953) noticed that distant galaxies had their spectrum red-shifted a greater amount from those of nearby galaxies.





distance

As explained by Christian Doppler (1803-1853), the red-shift of galaxies indicated that distance to these galaxies increased with

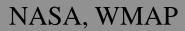
Inflation

Quantum Fluctuations

> 1st Stars about 400 million yrs.

> > **Big Bang Expansion**

13.7 billion years



WMAP

This led to the famous **Big Bang** model of the expanding universe, which has now been confirmed by many other cosmological observations.



Quantum Fluctuations

> 1st Stars about 400 million yrs.

> > **Big Bang Expansion**

13.7 billion years



WMAP

But it also gave a way to measure distances even at extremely large scales... by first measuring the red-shift and then applying Hubble's law.

A. S.

Red shift -

Spectroscopy

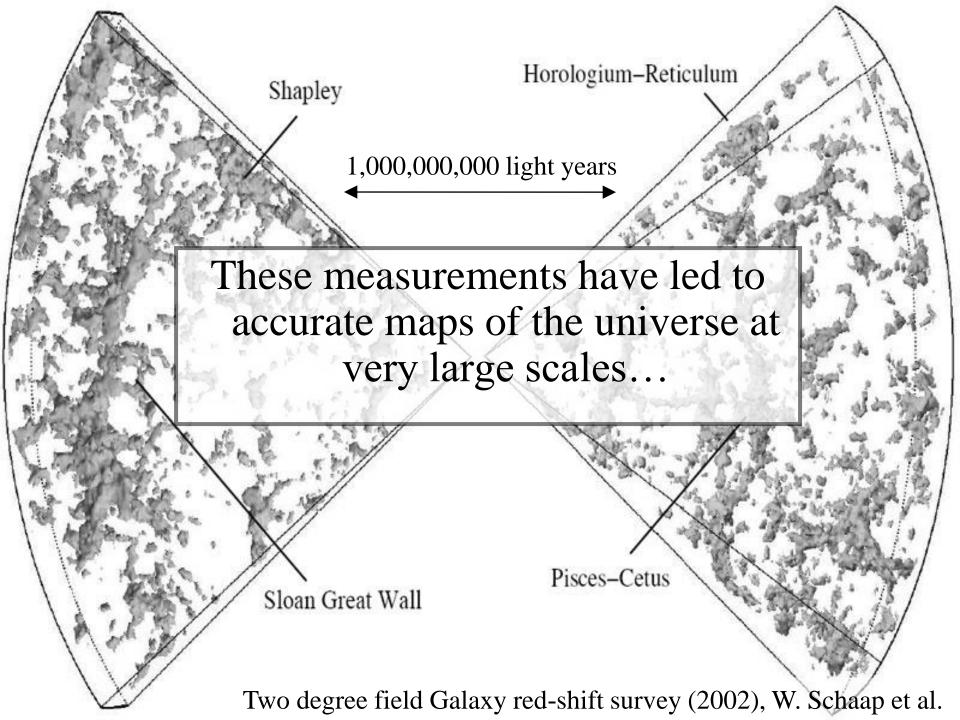
Speed of light

→ Recession velocity

Hubble deep field, NASA

Hubble's law

→ Distance



Horologium-Reticulum

1,000,000,000 light years

Shapley

Sloan Great Wall

which have led in turn to many discoveries of very large-scale structures, such as the Great Wall.

Pisces-Cetus

Two degree field Galaxy red-shift survey, W. Schaap et al.

For instance, our best estimate (as of 2004) of the current diameter of the entire universe is that it is at least 78 billion light-years.

Most distant object detected (gamma ray burst) : 13 billion light years Diameter of observable universe = 28 billion light years Diameter of entire universe > 78 billion light years (4.6×10^{23} mi) Age of universe = 13.7 billion years

Cosmic microwave background fluctuation, Planck cosmology probe

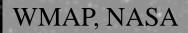
The mathematics becomes more advanced at this point, as the effects of general relativity have highly influenced the data we have at this scale of the universe.

Artist's rendition of a black hole, NASA

Cutting-edge technology (such as the Hubble space telescope (1990-) and WMAP (2001-2010)) has also been vital to this effort.

Hubble telescope, NASA

Climbing this rung of the ladder (i.e. mapping the universe at its very large scales) is still a very active area in astronomy today!



For instance, a stunning confirmation of the cosmic distance ladder calculations came in 2015 when the Laser Interferometer Gravitational Wave Observatory (LIGO) made the first detection in history of a black hole collision.

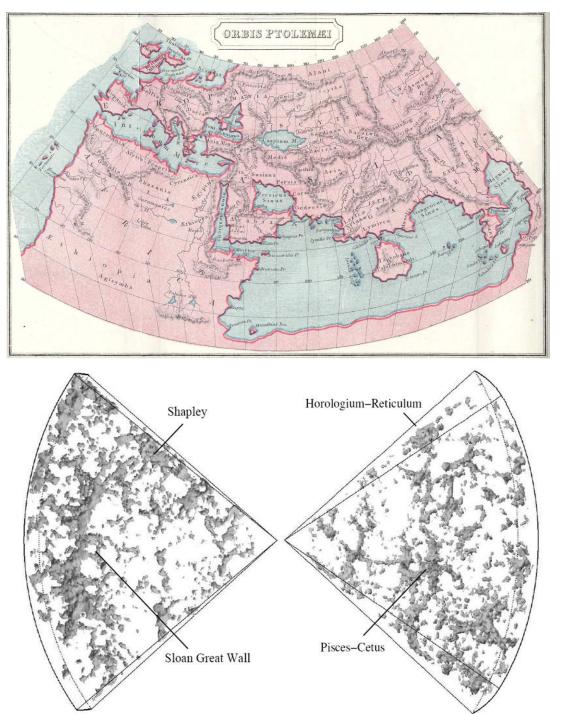


By comparing the theoretical strength of the gravitational wave predicted by general relativity with the actual signal received, the LIGO collaboration was able to directly measure the distance to the black holes as 1.4 billion light years – without any use of the distance ladder whatsoever!

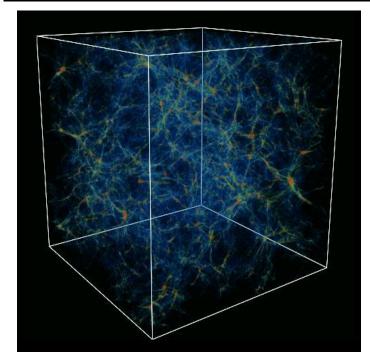
Artist's impression, NASA

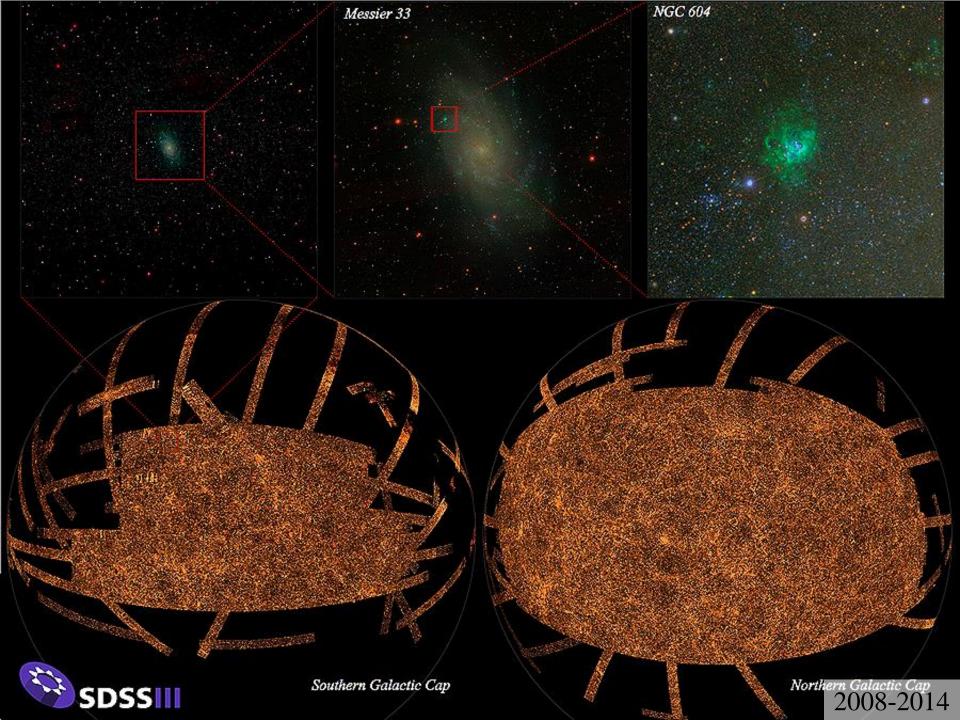
This measurement matched the one given by Hubble's law and the rest of the distance ladder to within ten percent. (Astronomers are still debating the implications of that ten percent deviation.)

Artist's impression, NASA









Celestial object	Distance (metres)	First (relative) measurement
Earth	1.2 x 10 ⁷ (diameter)	Eratosthenes (~240BCE)
Moon	$3.6 \ge 10^8$	Aristarchus (~270BCE)
Sun	1.5 x 10 ¹¹	Aristarchus (~270BCE) Cook etc. (1761,1769)
Mars	2.3 x 10 ¹¹ (from Sun)	Copernicus (1543)
Saturn	1.5 x 10 ¹² (from Sun)	Copernicus (1543)
Pluto	7.4 x 10 ¹² (from Sun)	Tombaugh (1930)
Proxima Centauri	$4.0 \ge 10^{16}$	Alden (1928)
61 Cygni	1.1 x 10 ¹⁷	Bessel (1838)
Hyades cluster	$1.4 \ge 10^{18}$	Smart (1939)
Pleiades cluster	$4.2 \ge 10^{18}$	Detweiler et al. (1984)
Galactic center	2.6 x 10 ²⁰	Shapley (1914)
Large Magellanic Cloud	$1.5 \ge 10^{21}$	Arp (1967)
Andromeda Galaxy	$2.4 \ge 10^{22}$	Hubble (1923)
NGC 4603	$1.0 \ge 10^{24}$	HST (1999)

Celestial object	Distance (metres)	First (relative) measurement
Sloan Great Wall	1.3 x 10 ²⁵ (diameter)	Gott et al. (2003)
1997ff Type Ia supernova	$1.0 \ge 10^{26}$	HST (1997)
GRB (Gamma Ray Burst) 090423	1.2 x 10 ²⁶	Swift satellite (2009)
UDFy-38135539 (Galaxy)	1.2 x 10 ²⁶	Lehnert et al. (2010)
Observable universe	2.8 x 10 ²⁶ (diameter)	Hubble (1929)
Entire universe	>7.2 x 10 ²⁶	Cornish et al. (2004)

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- 171: Henrietta Swan Leavitt Wikipedia
- 172-173: Leavitt's original Period-Brightness relation (X-axis in days, Y-axis in magnitudes) SAO/NASA
- 174-175: Refined Hubble Constant Narrows Possible Explanations for Dark Energy NASA/ESA/ A. Riess (STScl/JHU)
- 176: Rampaging Supernova Remnant N63A NASA/ESA/HEIC/The Hubble Heritage Team (STScl/AURA)
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- 188: Rotating Earth Wikipedia

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